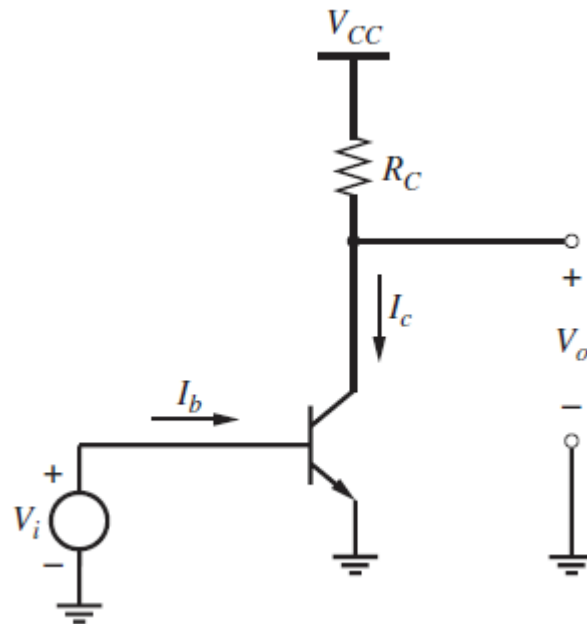


# Osnove elektronike

## III semestar

**AKTIVNO OPTEREĆENJE**

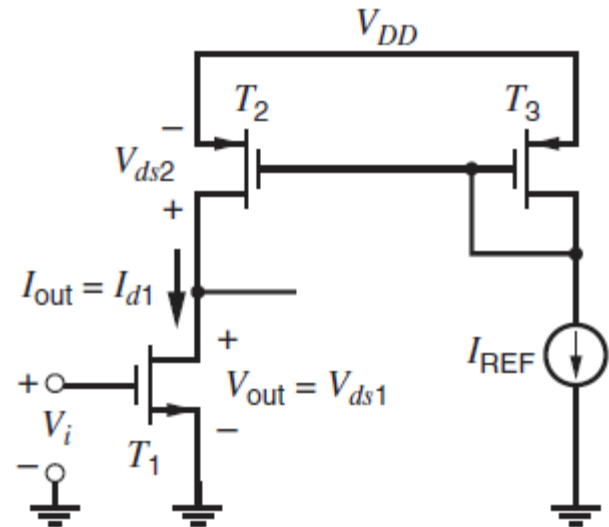
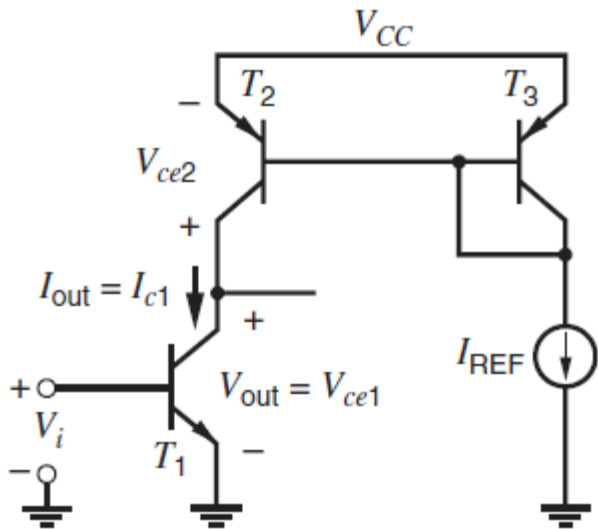
# Ograničenje pojačanja pojačavača sa otpornim opterećenjem



$$A_n = -g_m R_C = -\frac{I_C R_C}{V_T} \approx -\frac{V_{CC}}{2V_T}$$

Naponsko pojačanje pojačavača sa otpornim opterećenjem je ograničeno naponom napajanja.

# Aktivno opterećenje sa bipolarnim i MOS tranzistorima



$$i_{C1} = i_{C2}$$

$$i_{C3} = I_{REF}$$

$$v_{BE1} = v_i$$

$$v_{EB2} = v_{EB3}$$

$$v_{CE1} = v_{out}$$

$$v_{EC3} = v_{EB3}$$

$$v_{EC2} = V_{CC} - v_{CE1}$$

$$I_{S2} = I_{S3}$$

# Prenosna karakteristika pojačavača sa aktivnim opterećenjem

$$i_{C1} = I_{S1} \left( e^{\frac{v_{BE1}}{V_T}} - 1 \right) \left( 1 + \frac{v_{CE1}}{V_{AN}} \right) = I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \left( 1 + \frac{v_{out}}{V_{AN}} \right)$$

$$i_{C2} = I_{S2} \left( e^{\frac{v_{EB2}}{V_T}} - 1 \right) \left( 1 + \frac{v_{EC2}}{V_{AP}} \right) = I_{S2} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{V_{CC} - v_{out}}{V_{AP}} \right)$$

$$i_{C3} = I_{S3} \left( e^{\frac{v_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{v_{EC3}}{V_{AP}} \right) = I_{S3} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{V_{EB3}}{V_{AP}} \right)$$

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \left( 1 + \frac{v_{out}}{V_{AN}} \right) = I_{S2} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{V_{CC} - v_{out}}{V_{AP}} \right)$$

$$I_{REF} = I_{S3} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{V_{EB3}}{V_{AP}} \right) = I_{S2} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) \left( 1 + \frac{V_{EB3}}{V_{AP}} \right)$$

$$I_{S2} \left( e^{\frac{V_{EB3}}{V_T}} - 1 \right) = \frac{I_{REF}}{1 + \frac{V_{EB3}}{V_{AP}}}$$

# Prenosna karakteristika pojačavača sa aktivnim opterećenjem

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \left( 1 + \frac{v_{out}}{V_{AN}} \right) = \frac{I_{REF}}{1 + \frac{V_{EB3}}{V_{AP}}} \left( 1 + \frac{V_{CC} - v_{out}}{V_{AP}} \right)$$

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) = I_{REF} \frac{1 + \frac{V_{CC} - v_{out}}{V_{AP}}}{\left( 1 + \frac{V_{EB3}}{V_{AP}} \right) \left( 1 + \frac{v_{out}}{V_{AN}} \right)}$$

$$\frac{V_{EB3}}{V_{AP}} \ll 1 \quad \frac{v_{out}}{V_{AN}} \ll 1$$

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \approx I_{REF} \left( 1 + \frac{V_{CC} - v_{out}}{V_{AP}} \right) \left( 1 - \frac{V_{EB3}}{V_{AP}} \right) \left( 1 - \frac{v_{out}}{V_{AN}} \right)$$

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \approx I_{REF} \left( 1 + \frac{V_{CC} - v_{out}}{V_{AP}} - \frac{V_{EB3}}{V_{AP}} - \frac{v_{out}}{V_{AN}} \right)$$

$$I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right) \approx I_{REF} \left[ 1 + \frac{V_{CC} - V_{EB3}}{V_{AP}} - v_{out} \left( \frac{1}{V_{AP}} + \frac{1}{V_{AN}} \right) \right]$$

# Prenosna karakteristika pojačavača sa aktivnim opterećenjem

$$\frac{I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right)}{I_{REF}} \approx 1 + \frac{V_{CC} - V_{EB3}}{V_{AP}} - v_{out} \left( \frac{1}{V_{AP}} + \frac{1}{V_{AN}} \right)$$

$$v_{out} \left( \frac{1}{V_{AP}} + \frac{1}{V_{AN}} \right) \approx 1 + \frac{V_{CC} - V_{EB3}}{V_{AP}} - \frac{I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right)}{I_{REF}}$$

$$v_{out} \approx \frac{\frac{V_{CC} - V_{EB3}}{V_{AP}} + 1 - \frac{I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right)}{I_{REF}}}{\frac{1}{V_{AP}} + \frac{1}{V_{AN}}}$$

$$v_{out} \approx \frac{\frac{V_{CC} - V_{EB3}}{V_{AP}} + 1 - \frac{I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right)}{I_{REF}}}{\frac{V_{AP} + V_{AN}}{V_{AP} V_{AN}}}$$

# Naponsko pojačanje pojačavača sa aktivnim opterećenjem

$$v_{out} \approx (V_{CC} - V_{EB3}) \frac{V_{AN}}{V_{AP} + V_{AN}} + \frac{V_{AN}V_{AP}}{V_{AP} + V_{AN}} \left[ 1 - \frac{I_{S1} \left( e^{\frac{v_i}{V_T}} - 1 \right)}{I_{REF}} \right]$$

$$A_n = \frac{dv_{out}}{dv_i} \approx - \frac{V_{AN}V_{AP}}{V_{AP} + V_{AN}} \frac{I_{S1} e^{\frac{v_i}{V_T}}}{I_{REF}} \frac{1}{V_T}$$

$$\frac{I_{S1} e^{\frac{v_i}{V_T}}}{I_{REF}} = 1$$

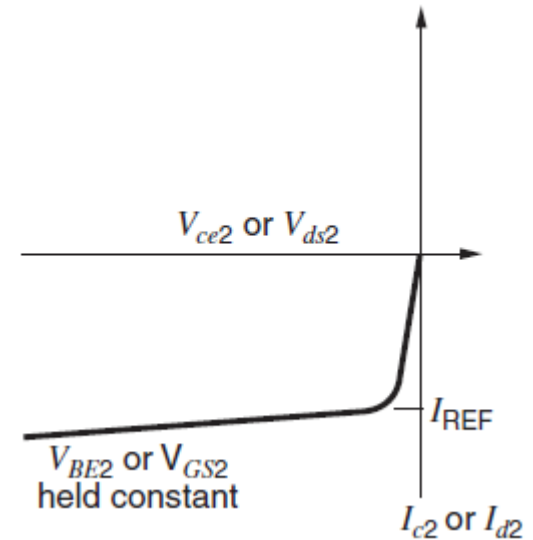
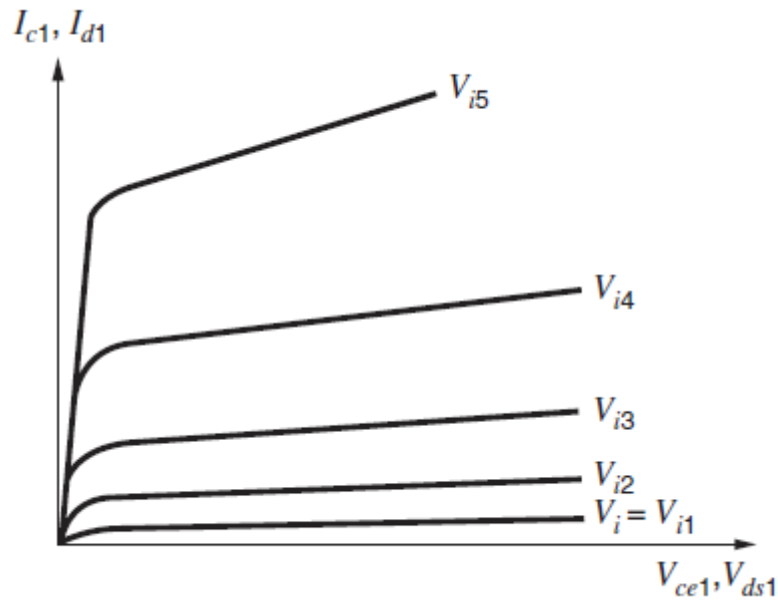
$$A_n = \frac{dv_{out}}{dv_i} \approx - \frac{V_{AN}V_{AP}}{V_{AP} + V_{AN}} \frac{1}{V_T}$$

$$A_n = \frac{dv_{out}}{dv_i} \approx - \frac{1}{\frac{V_T}{V_{AP}} + \frac{V_T}{V_{AN}}}$$

Naponsko pojačanje pojačavača sa aktivnim opterećenjem je nezavisno od napona napajanja.

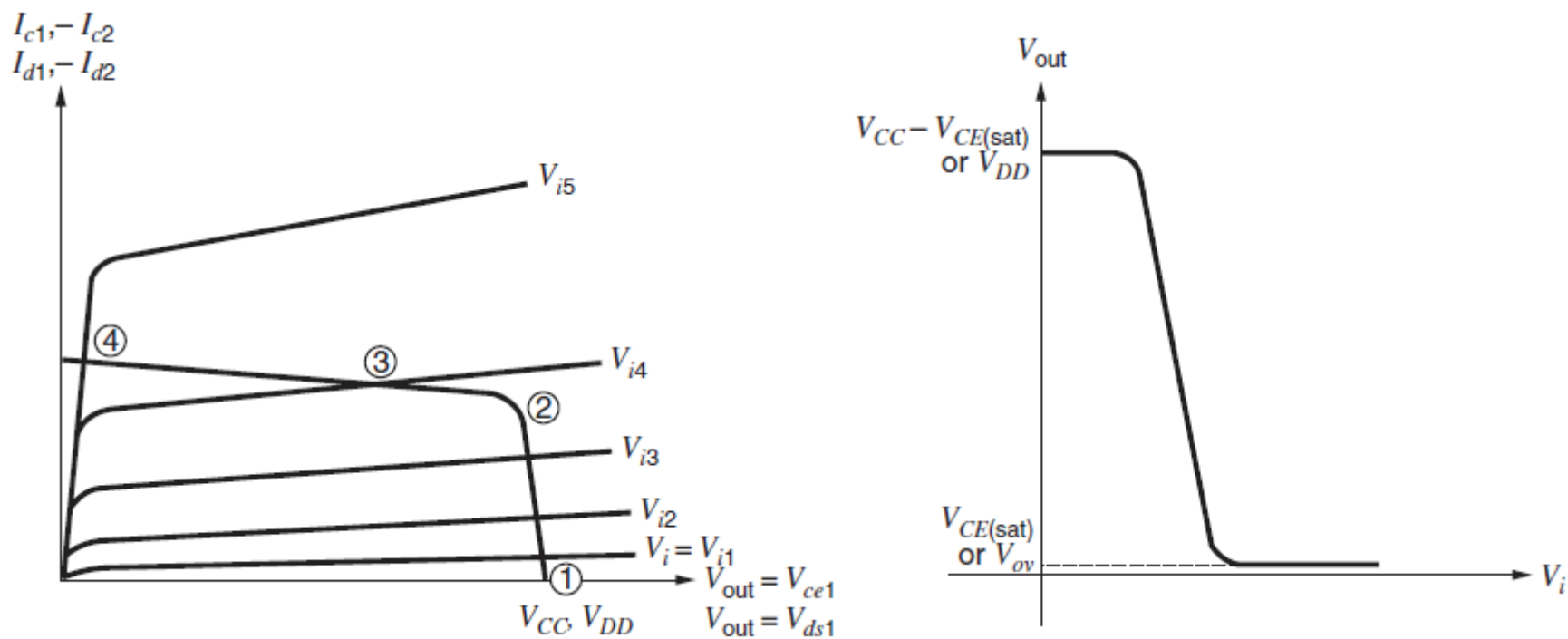


# Strujno-naponska karakteristika ulaznog tranzistora i aktivnog opterećenja

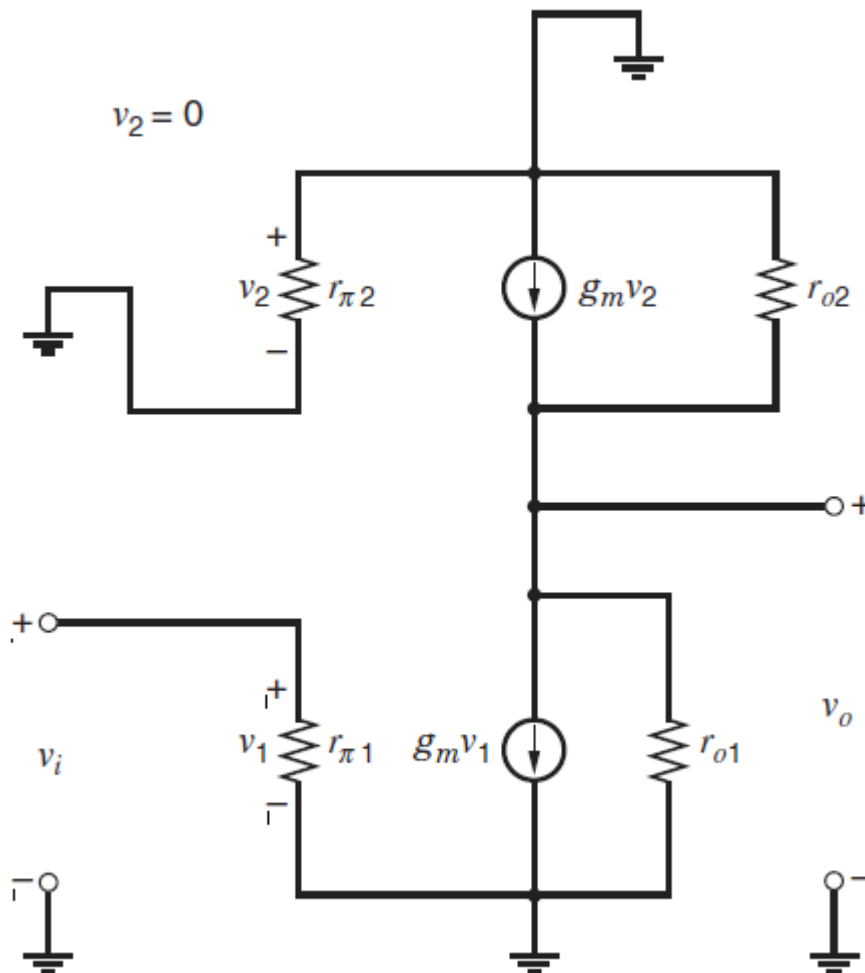




# Superponirane strujno-naponske karakteristike ulaznog tranzistora i aktivnog opterećenja, kao i prenosna karakteristika



# Šema za male signale pojačavača sa aktivnim opterećenjem



$$R_o = r_{o1} || r_{o2}$$

$$A_v = -g_{m1}(r_{o1} || r_{o2})$$

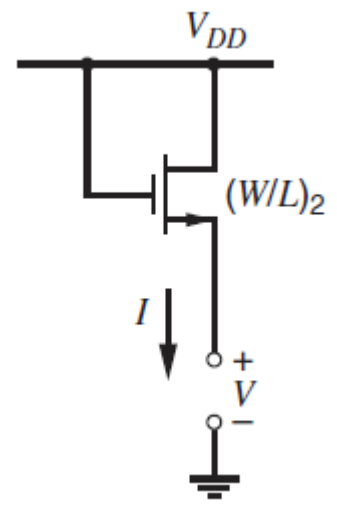
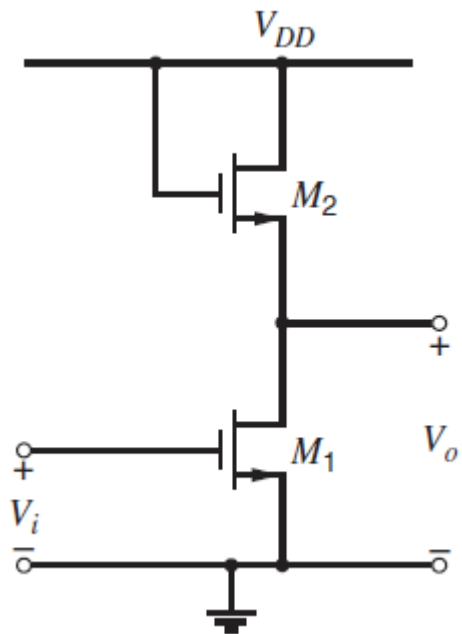
$$A_v = -\frac{1}{\frac{V_T}{V_{A1}} + \frac{V_T}{V_{A2}}}$$

Ista šema važi za MOSFET ako se izbace ulazne otpornosti:

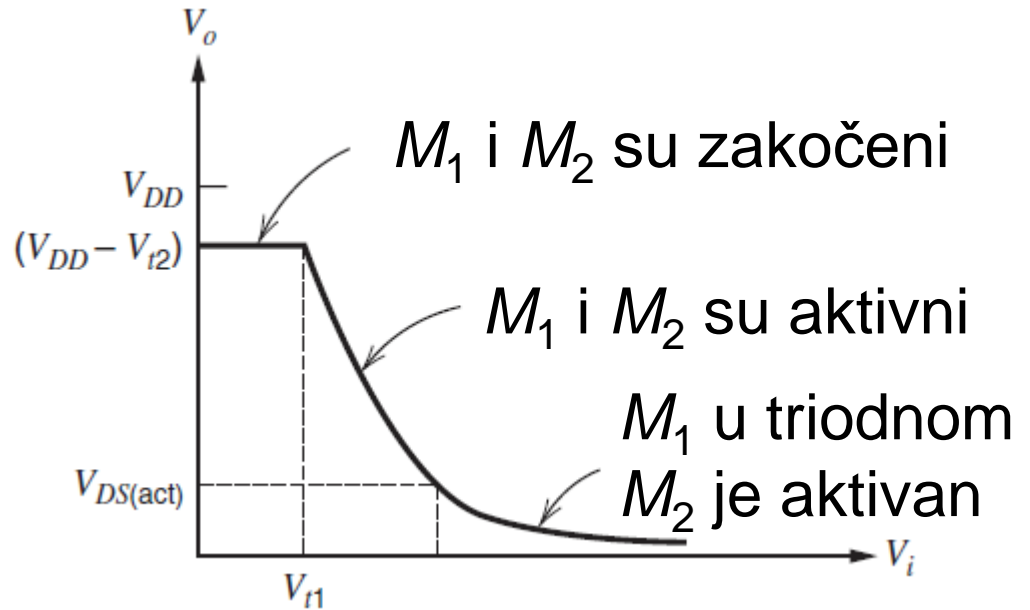
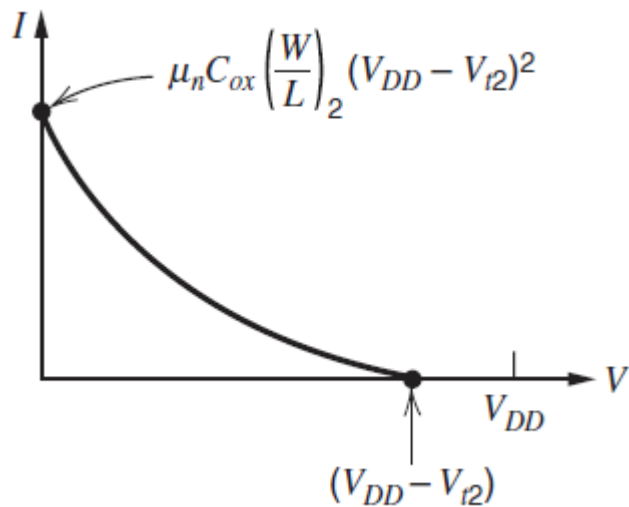
$$r_{\pi 1} \rightarrow \infty$$

$$r_{\pi 2} \rightarrow \infty$$

# Pojačavač sa MOSFET-om i kolo za određivanje struje



# Struja i prenosna karakteristika pojačavača sa MOSFET-om



# Izlazni napon pojačavača sa MOSFET-om

$$i_{D1} = \frac{B_1}{2} (v_{GS1} - V_{T1})^2 \quad B_1 = \frac{\mu_n C_{ox} W_1}{L_1} \quad v_{GS1} = V_{T1} + \sqrt{\frac{2i_{D1}}{B_1}}$$

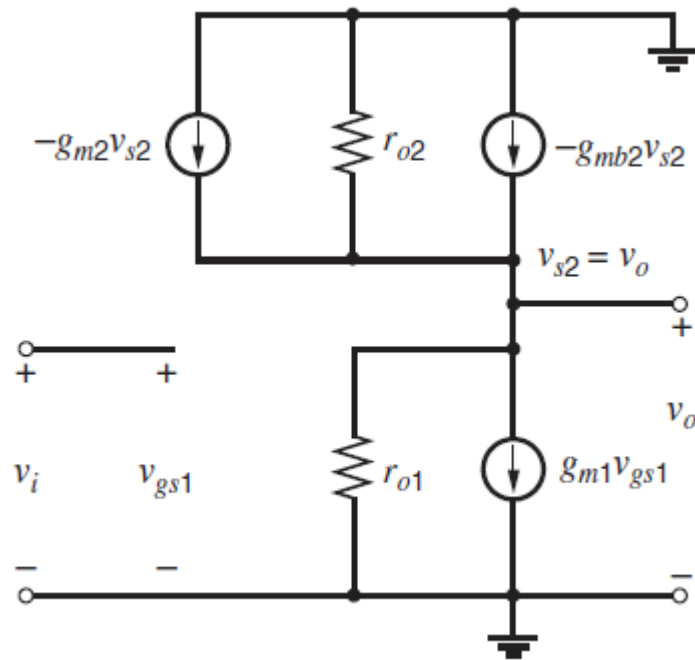
$$i_{D2} = \frac{B_2}{2} (v_{GS2} - V_{T2})^2 \quad B_2 = \frac{\mu_p C_{ox} W_2}{L_2} \quad v_{GS2} = V_{T2} + \sqrt{\frac{2i_{D2}}{B_2}}$$

$$v_o = V_{DD} - v_{GS2} \quad v_o = V_{DD} - V_{T2} - \sqrt{\frac{2i_{D2}}{B_2}} \quad i_{D2} = i_{D1}$$

$$v_o = V_{DD} - V_{T2} - \sqrt{\frac{2i_{D1}}{B_2}} \quad \sqrt{\frac{2i_{D1}}{B_1}} = v_{GS1} - V_{T1} \quad v_{GS1} = v_i$$

$$v_o = V_{DD} - V_{T2} - \sqrt{\frac{B_1}{B_2}} (v_{GS1} - V_{T1}) \quad v_o = V_{DD} - V_{T2} - \sqrt{\frac{(W/L)_1}{(W/L)_2}} (v_i - V_{T1})$$

# Šema za male signale pojačavača sa MOSFET-om



# Pojačanje za male signale pojačavača sa MOSFET-om

$$g_{m1}v_i + \frac{v_o}{r_{o1}} + \frac{v_o}{r_{o2}} + g_{m2}v_o + g_{mb2}v_o = 0$$

$$\frac{v_o}{v_i} = -g_{m1} \left( \frac{1}{g_{m2}} \parallel \frac{1}{g_{mb2}} \parallel r_{o1} \parallel r_{o2} \right) = -\frac{g_{m1}}{g_{m2}} \left( \frac{1}{1 + \frac{g_{mb2}}{g_{m2}} + \frac{1}{g_{m2}r_{o1}} + \frac{1}{g_{m2}r_{o2}}} \right)$$

$$g_{m2}/g_{mb2} \gg 1$$

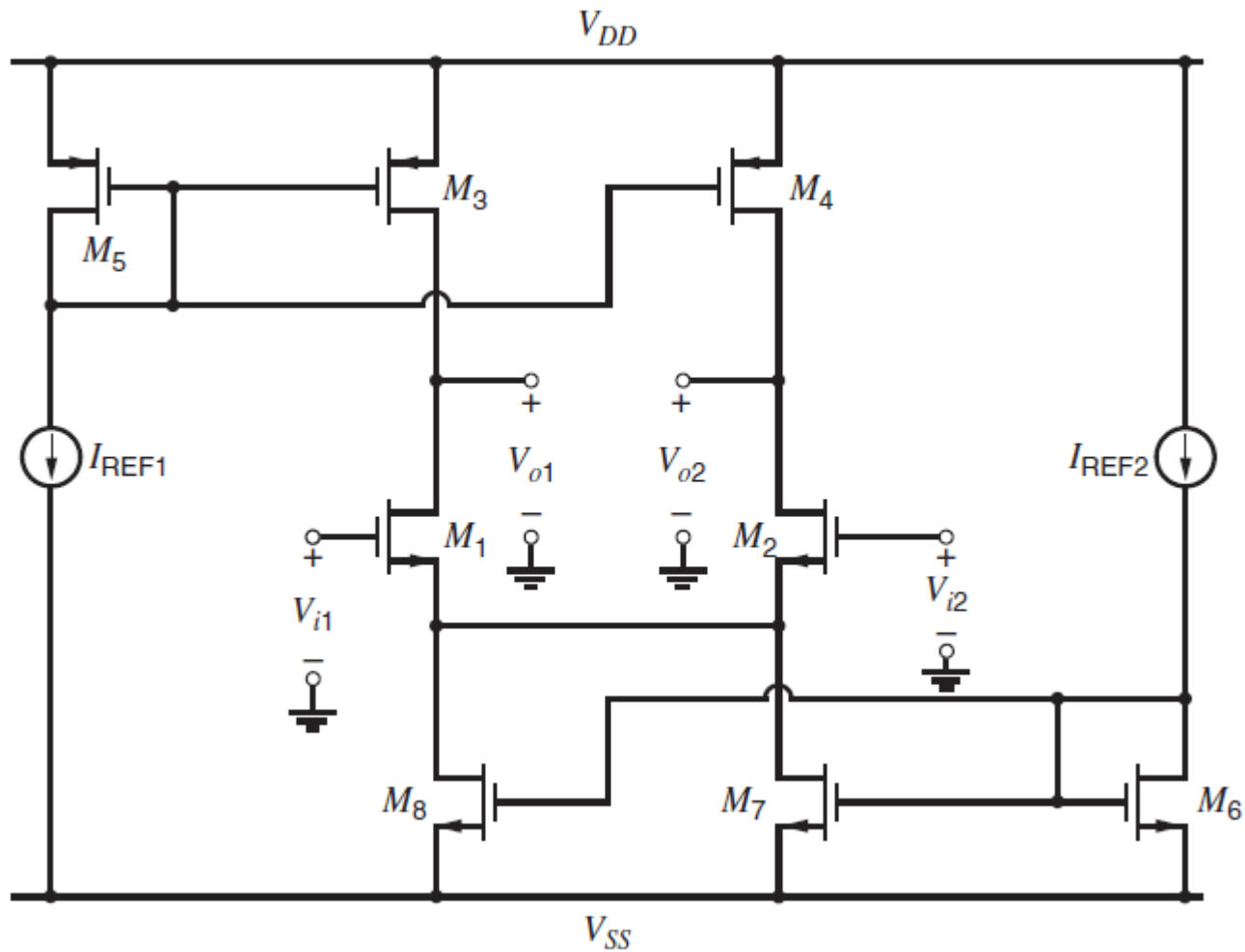
$$g_{m2}r_{o1} \gg 1$$

$$g_{m2}r_{o2} \gg 1$$

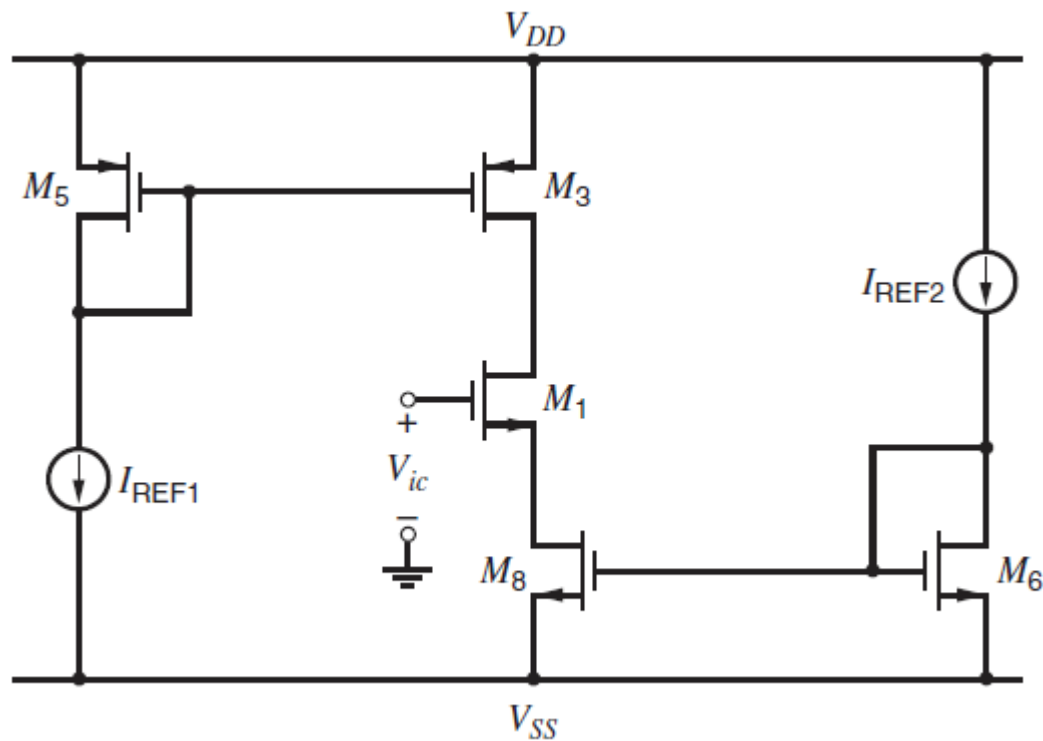
$$\frac{v_o}{v_i} \simeq -\frac{g_{m1}}{g_{m2}} = -\sqrt{\frac{(W/L)_1}{(W/L)_2}}$$



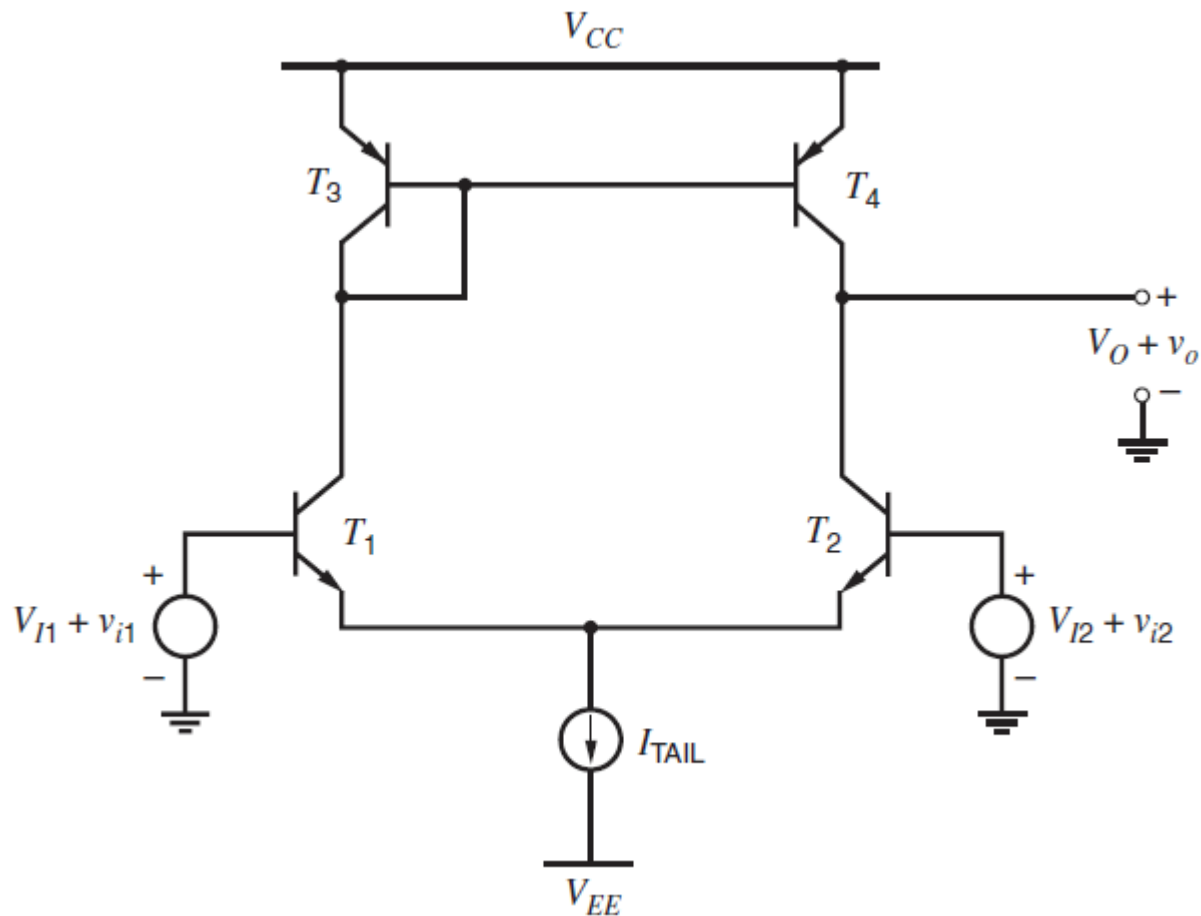
# Diferencijalni par sa aktivnim opterećenjem



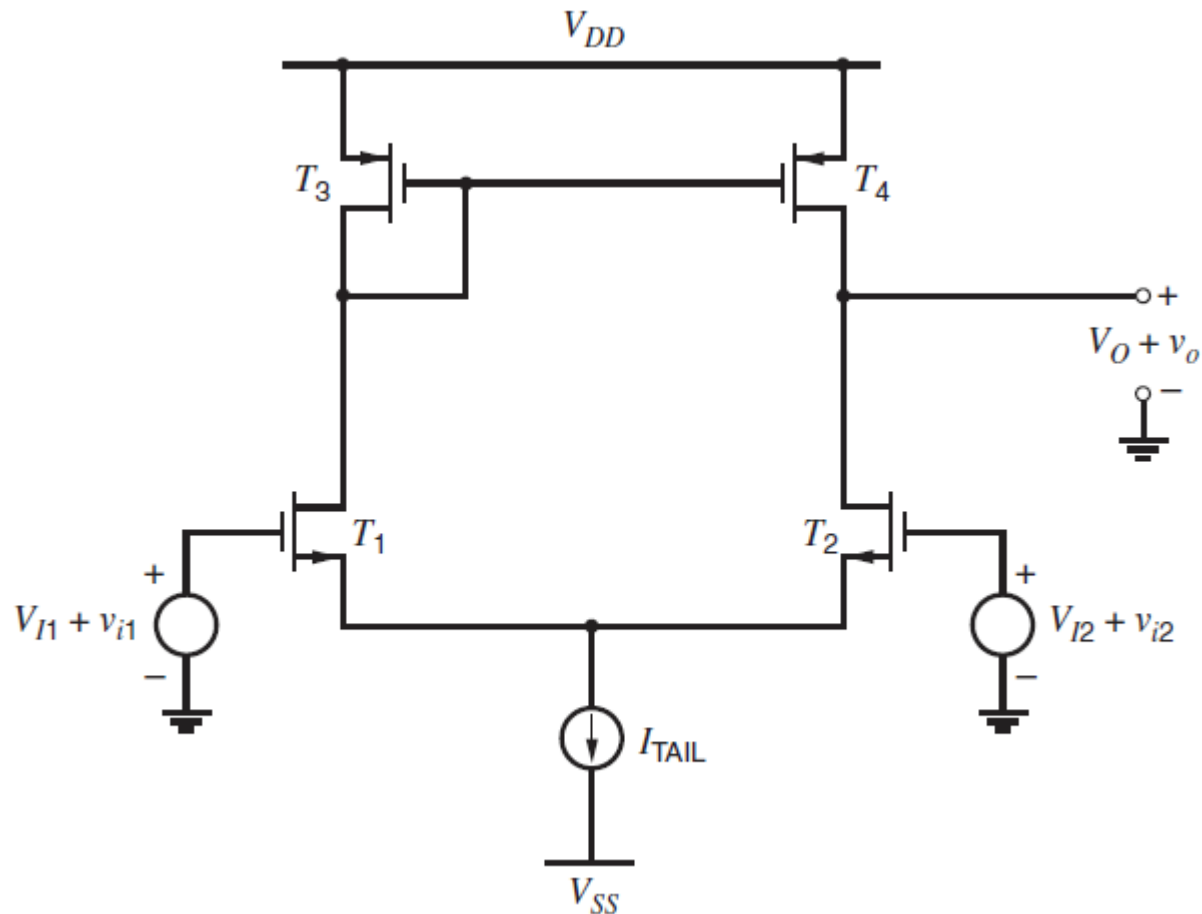
# Polovina diferencijalnog para sa aktivnim opterećenjem



# Diferencijalni par sa aktivnim opterećenjem za svodjenje na jednostruki izlaz



# Diferencijalni par sa aktivnim opterećenjem za svodjenje na jednostruki izlaz



# Šema za male signale diferencijalnog para sa aktivnim opterećenjem i jednostrukim izlazom

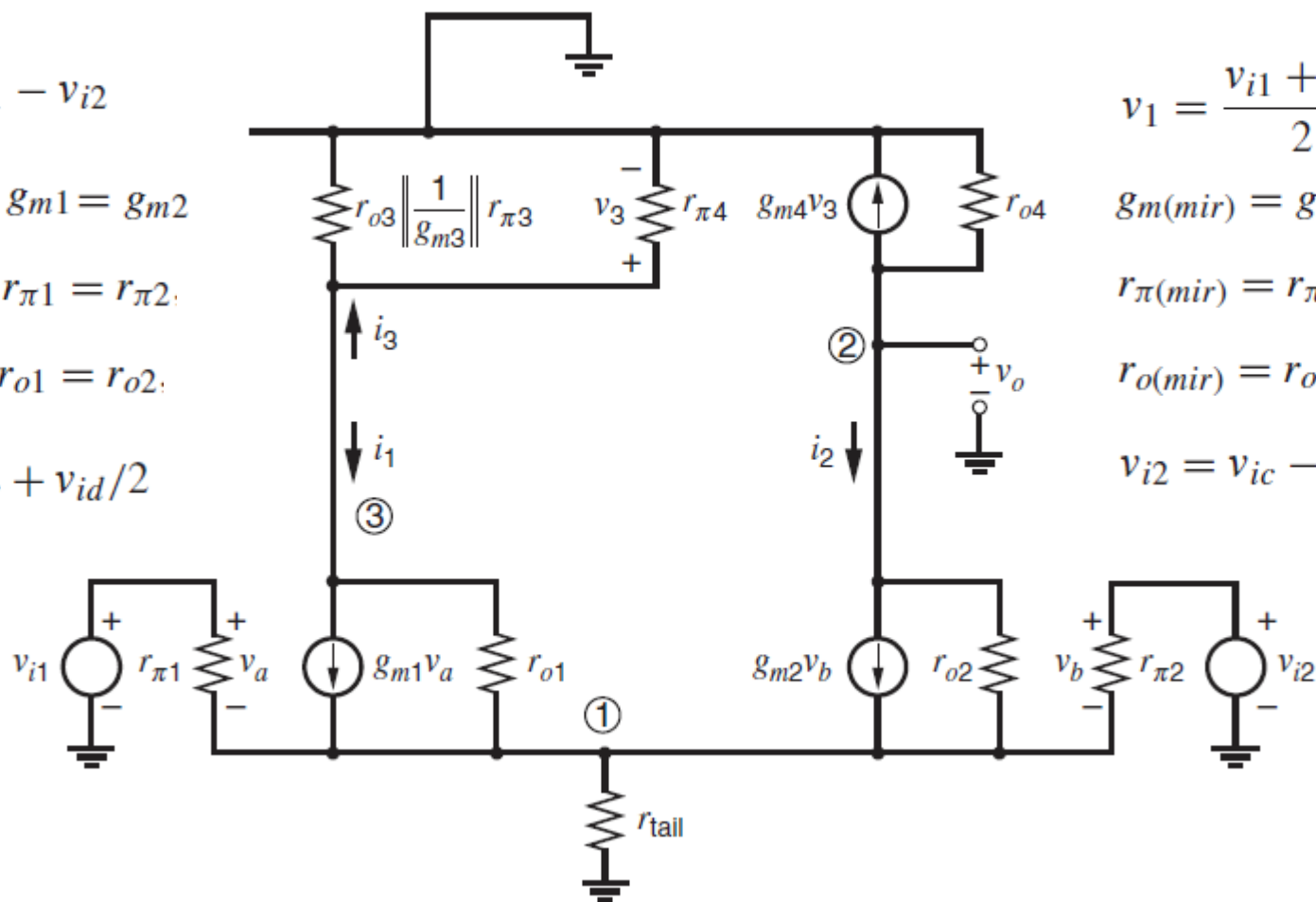
$$v_{id} = v_{i1} - v_{i2}$$

$$g_{m(dp)} = g_{m1} = g_{m2}$$

$$r_{\pi(dp)} = r_{\pi1} = r_{\pi2}$$

$$r_{o(dp)} = r_{o1} = r_{o2}$$

$$v_{i1} = v_{ic} + v_{id}/2$$



$$v_1 = \frac{v_{i1} + v_{i2}}{2} = v_{ic}$$

$$g_{m(mir)} = g_{m3} = g_{m4}$$

$$r_{\pi(mir)} = r_{\pi3} = r_{\pi4}$$

$$r_{o(mir)} = r_{o3} = r_{o4}$$

$$v_{i2} = v_{ic} - v_{id}/2$$

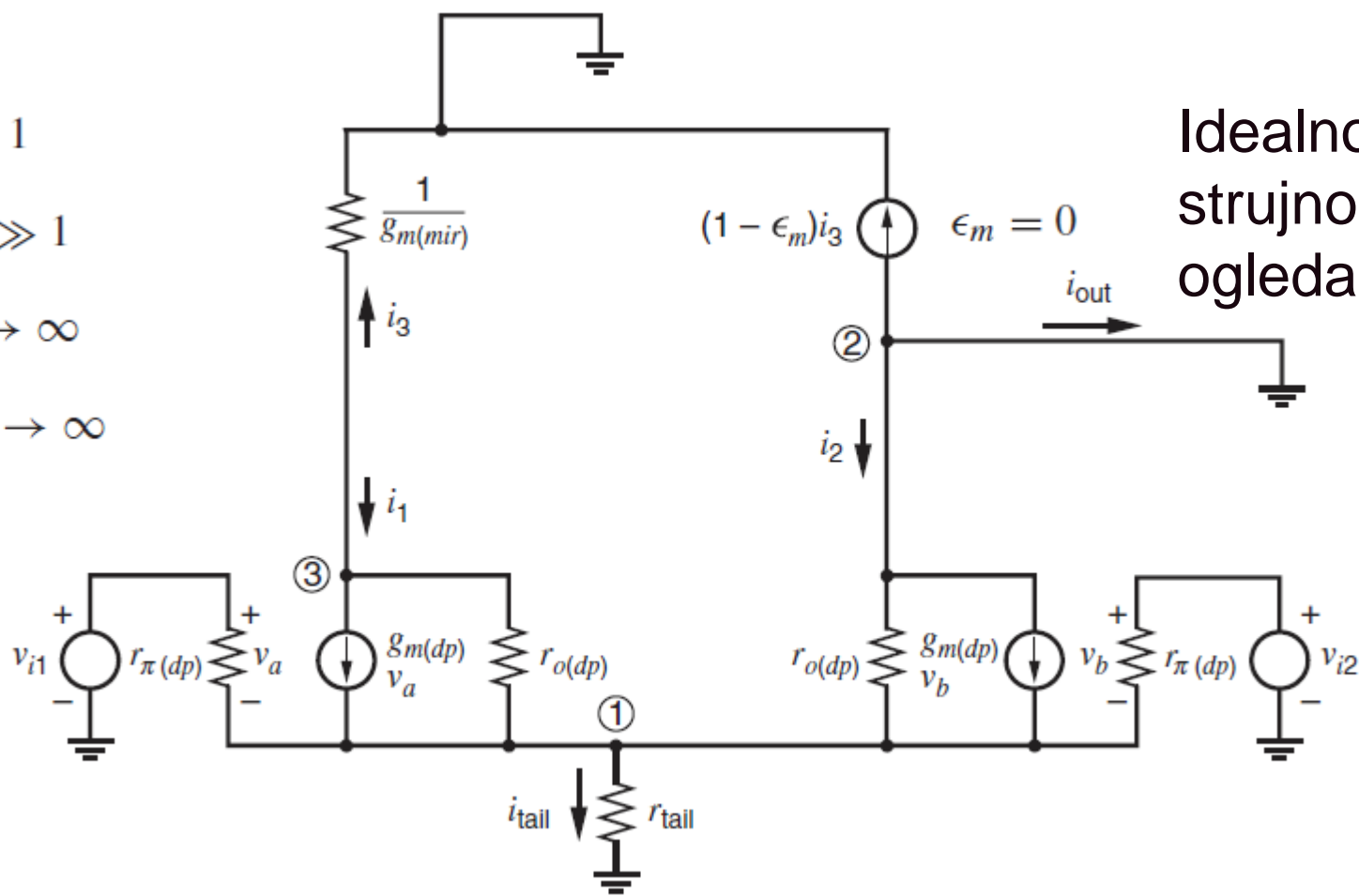
# Šema za male signale diferencijalnog para sa aktivnim opterećenjem i jednostrukim izlazom

$$\beta_0 \gg 1$$

$$g_m r_o \gg 1$$

$$r_{\text{tail}} \rightarrow \infty$$

$$r_{o(dp)} \rightarrow \infty$$



# Pojačanje za male signale diferencijalnog para sa aktivnim opterećenjem i jednostrukim izlazom

$$v_3 = i_3 r_3 \simeq \frac{i_3}{g_{m3}}$$

$$(v_{i1} - v_1 + v_{i2} - v_1) \left( \frac{1}{r_{\pi(dp)}} + g_{m(dp)} \right) + \frac{v_3 - v_1}{r_{o(dp)}} - \frac{v_1}{r_{o(dp)} || r_{tail}} = 0$$

$$i_1 = g_{m(dp)}(v_{i1} - v_1) = \frac{g_{m(dp)} v_{id}}{2}$$

$$i_2 = g_{m(dp)}(v_{i2} - v_1) = -\frac{g_{m(dp)} v_{id}}{2}$$

$$i_{out} = -(1 - \epsilon_m) i_3 - i_2$$

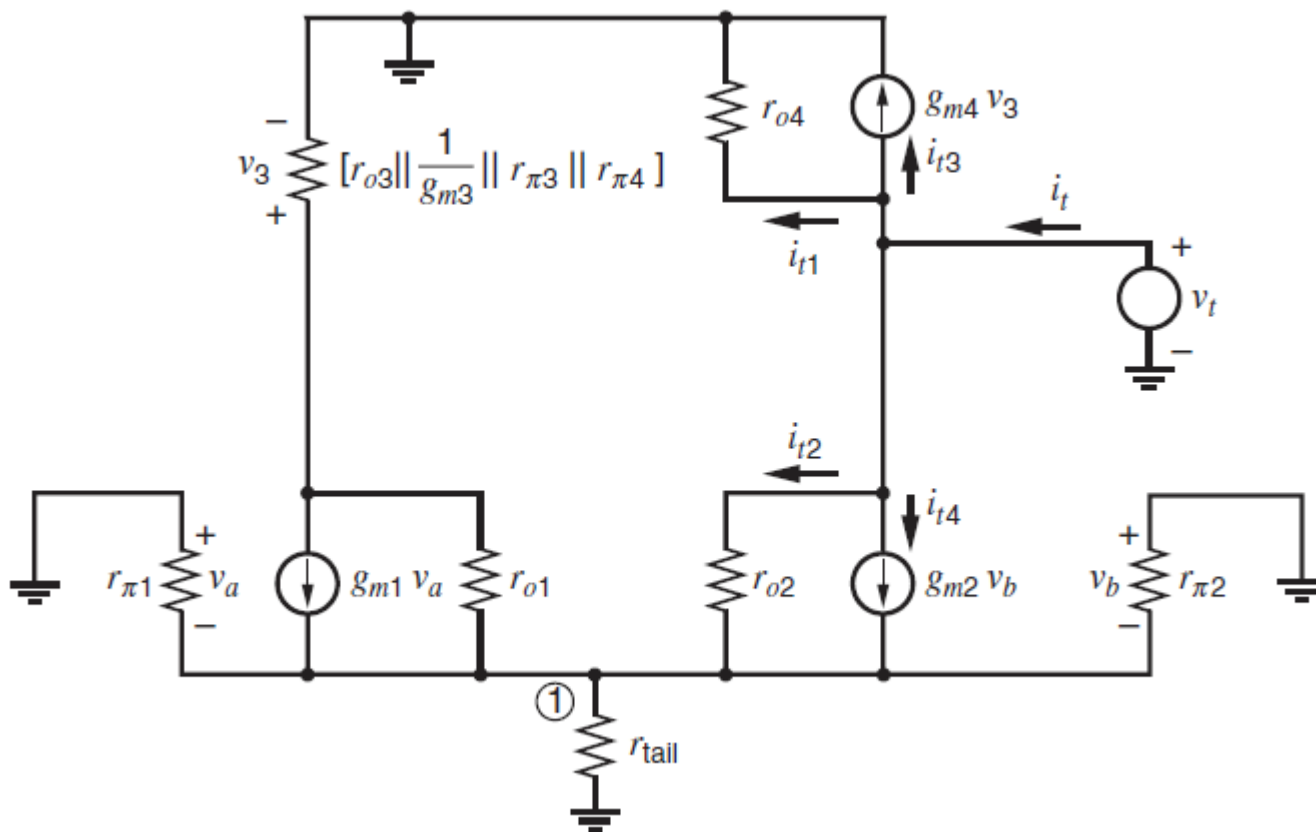
$$\epsilon_m = 0$$

$$i_3 = -i_1$$

$$i_{out} = g_{m(dp)} v_{id}$$



# Šema za određivanje izlazne otpornosti diferencijalnog para sa aktivnim opterećenjem



# Izlazna otpornost diferencijalnog para sa aktivnim opterećenjem i jednostrukim izlazom

$$i_{t1} = \frac{v_t}{r_{o4}}$$

$$R_{o2} \simeq r_{o2} \left( 1 + g_{m2} \frac{1}{g_{m1}} \right) = 2r_{o2}$$

Efektivna izlazna otpornost T2

$$i_{t2} + i_{t4} \simeq \frac{v_t}{2r_{o2}}$$

$$r_{\text{tail}} \gg 1/g_{m1}$$

$$i_{t3} \simeq i_{t2} + i_{t4} \simeq \frac{v_t}{2r_{o2}}$$

Strujno ogledalo T3 – T4.

$$i_t = i_{t1} + i_{t2} + i_{t3} + i_{t4} \simeq v_t \left( \frac{1}{r_{o4}} + \frac{1}{r_{o2}} \right)$$

$$r_{o2} = r_{o(dp)}$$

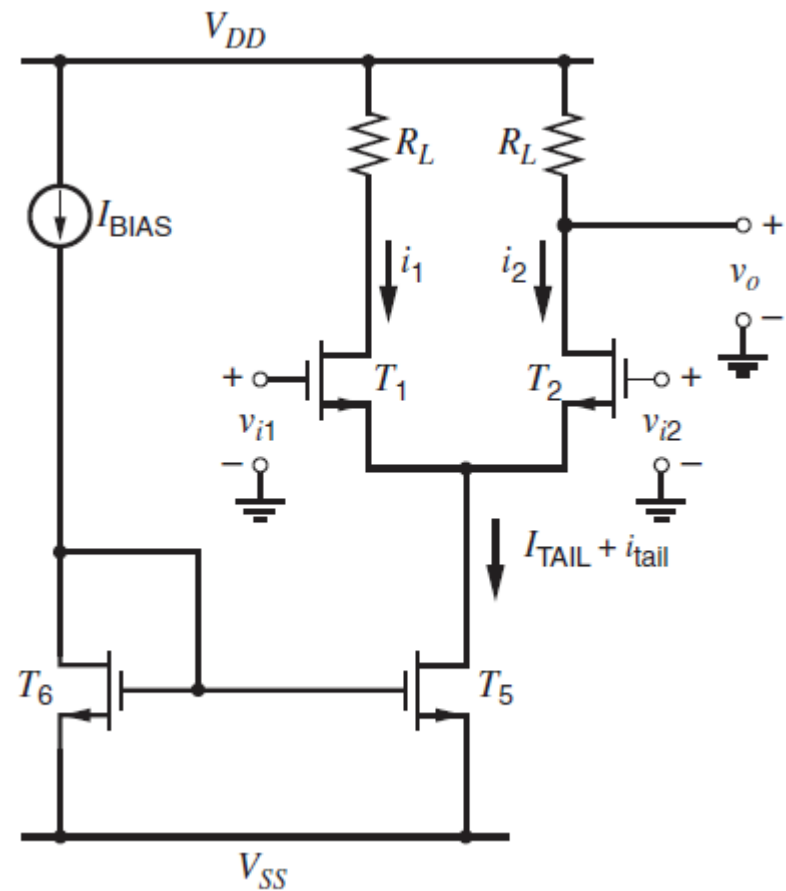
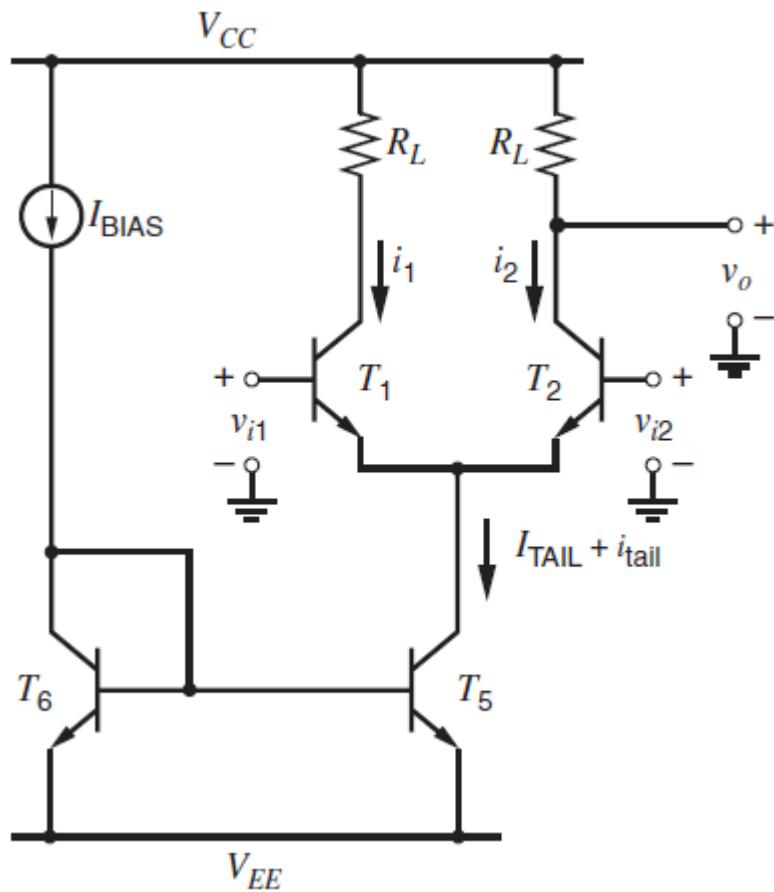
Diferencijalni  
pojačavač

$$R_o = \frac{v_t}{i_t} \Bigg|_{\substack{v_{i1}=0 \\ v_{i2}=0}} \simeq \frac{1}{\frac{1}{r_{o(dp)}} + \frac{1}{r_{o(mir)}}} = r_{o(dp)} || r_{o(mir)}$$

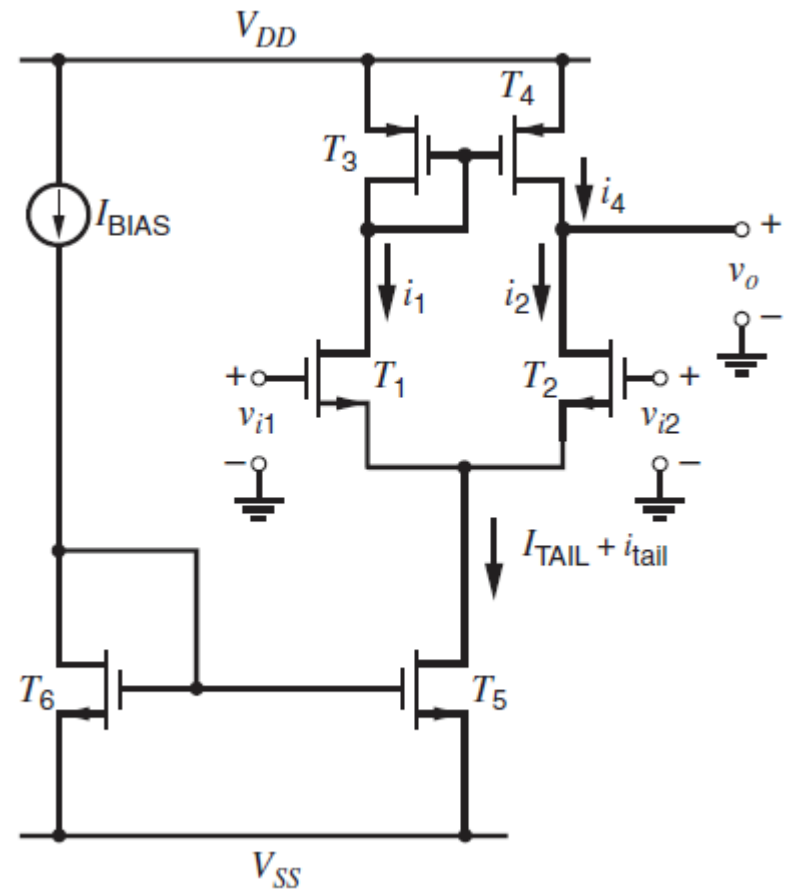
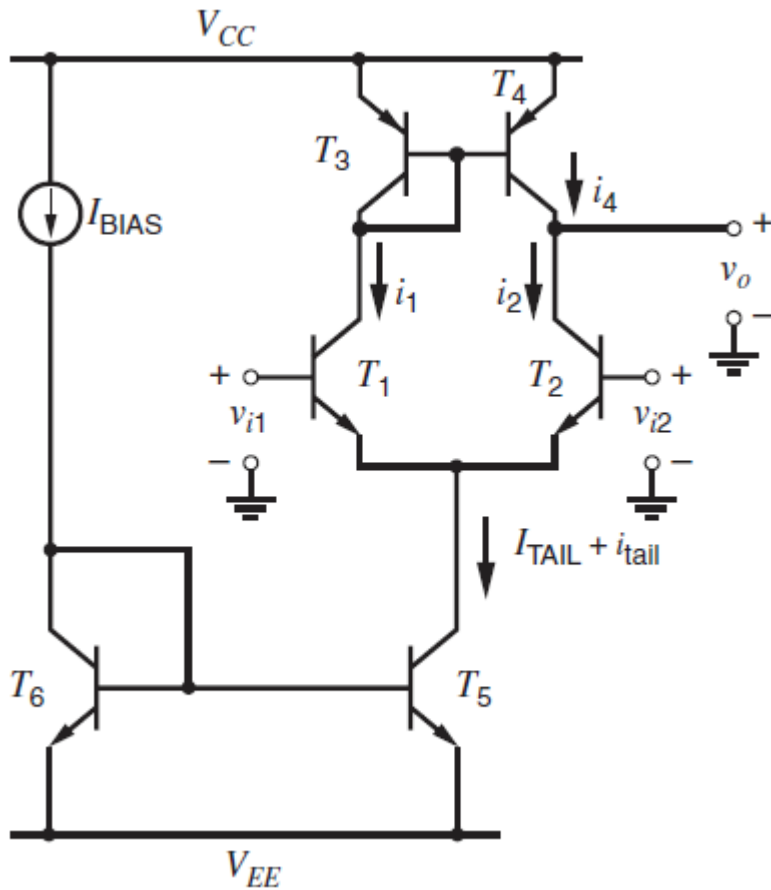
$$r_{o4} = r_{o(mir)}$$

Strujno  
ogledalo

# Diferencijalni par sa otpornim opterećenjem i jednostrukim izlazom



# Diferencijalni par sa aktivnim opterećenjem za svodenje na jednostruki izlaz



# Osnove elektronike

## III semestar

**AKTIVNO OPTEREĆENJE**