

# Sinteza električnih filtara

Dr Miroslav Lutovac

## Cilj predmeta

Savladati teorijske osnove  
analognih električnih filtara

Korišćenje računarskih alata  
za projektovanje filtara

# Ishod predmeta

- Da se na osnovu zahteva za rad uređaja
  - definišu specifikacije koje filter treba da zadovolji
  - da se izabere najbolja aproksimacija
  - da se izabere tehnologiju za implementaciju.
- Koristeći alate da se
  - projektuje filter (sinteza)
  - uradi simulacija
  - uradi optimizacija

# Teorijska nastava

- Uloga filtara u složenim sistemima i uređajima
- Izbor aproksimacione funkcije
- Projektovanje korišćenjem računarskih alata
- Realizacija filtara
  - aktivni sa operacionim pojačavačima
  - OTA
  - SS
  - pasivni filtri
  - univerzalna filterska integrisana kola
  - programabilna analogna kola

# Praktična nastava

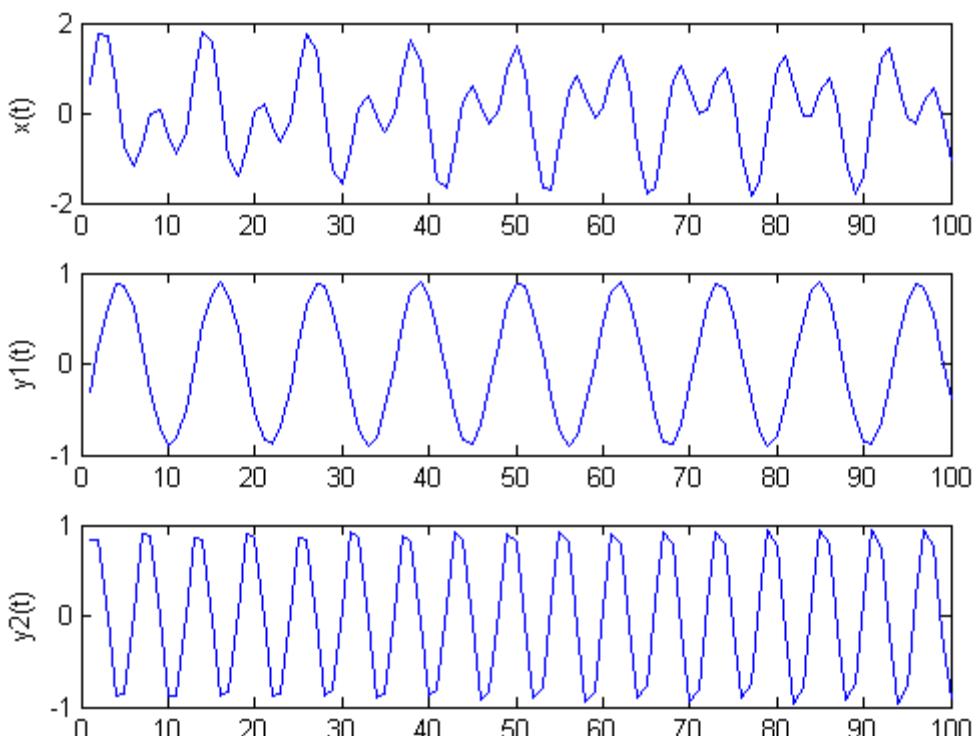
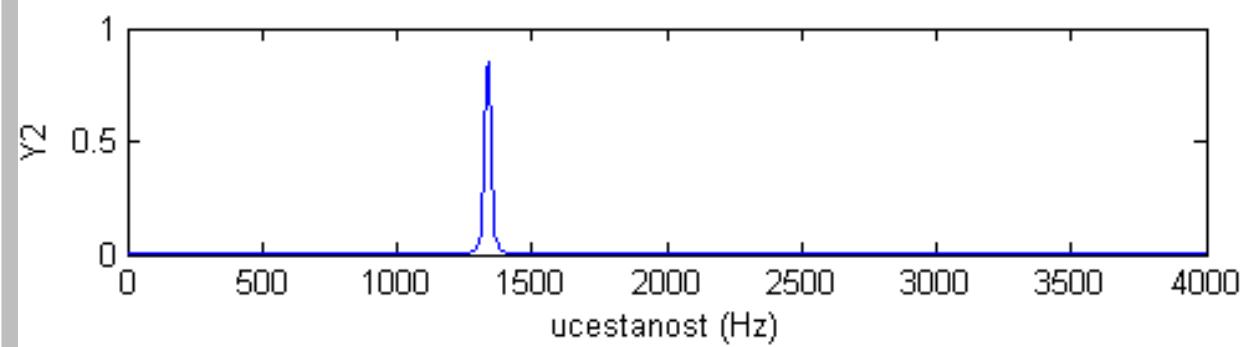
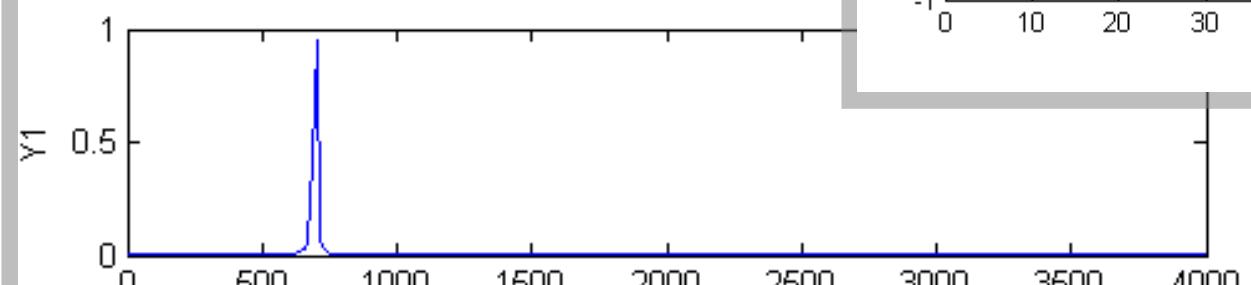
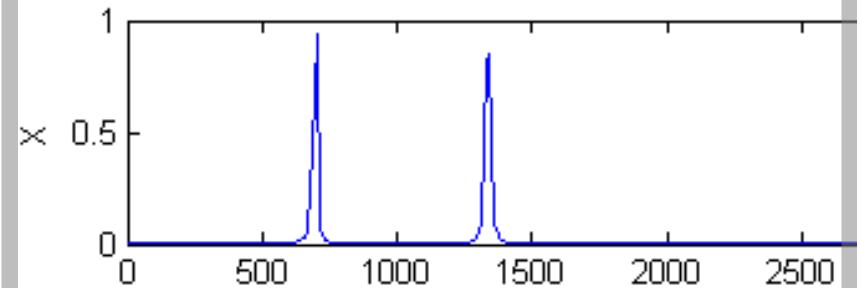
- Korišćenje standardnih računarskih alata za
  - projektovanje
  - analizu i
  - simulaciju
- rada električnih filtara

# Literatura

1. M. Lutovac, D. Tasic, B. Evans,  
**Filter Design for Signal Processing  
Using MATLAB and Mathematica**,  
Prentice Hall, New Jersey, 2001
2. G. Moschytz, P. Horn,  
**Active filter design handbook**,  
John Wiley, New York, 1981
3. G. Daryanani,  
**Principles of Active Network Synthesis  
and Design**,  
John Wiley, New York, 1976
4. **Anadigm**, Software user manual

# Telefon #2

## 697Hz + 1336 Hz

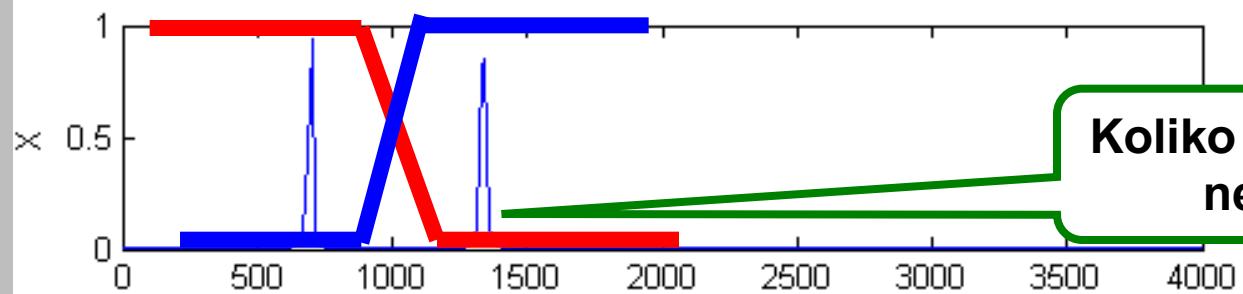


# Telefon #2

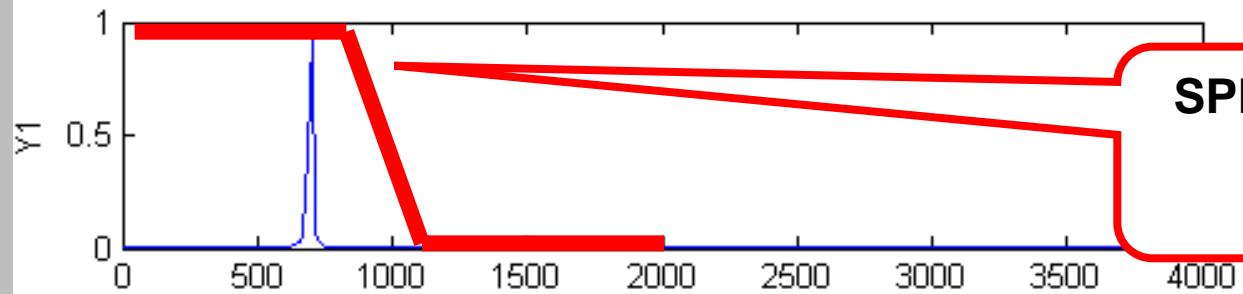
697Hz + 1336 Hz

697, 770, 852, 941 Hz

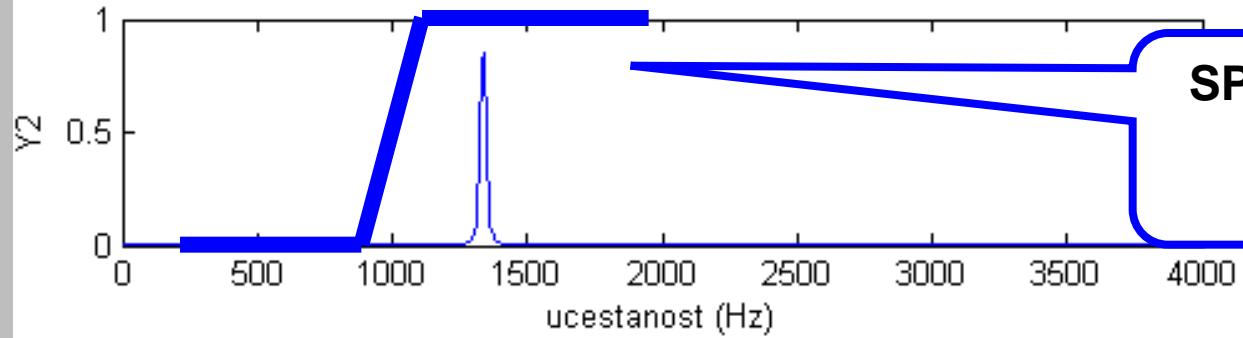
1209, 1336, 1477, 1633 Hz



Koliko da oslabimo signal na nekoj učestanosti?

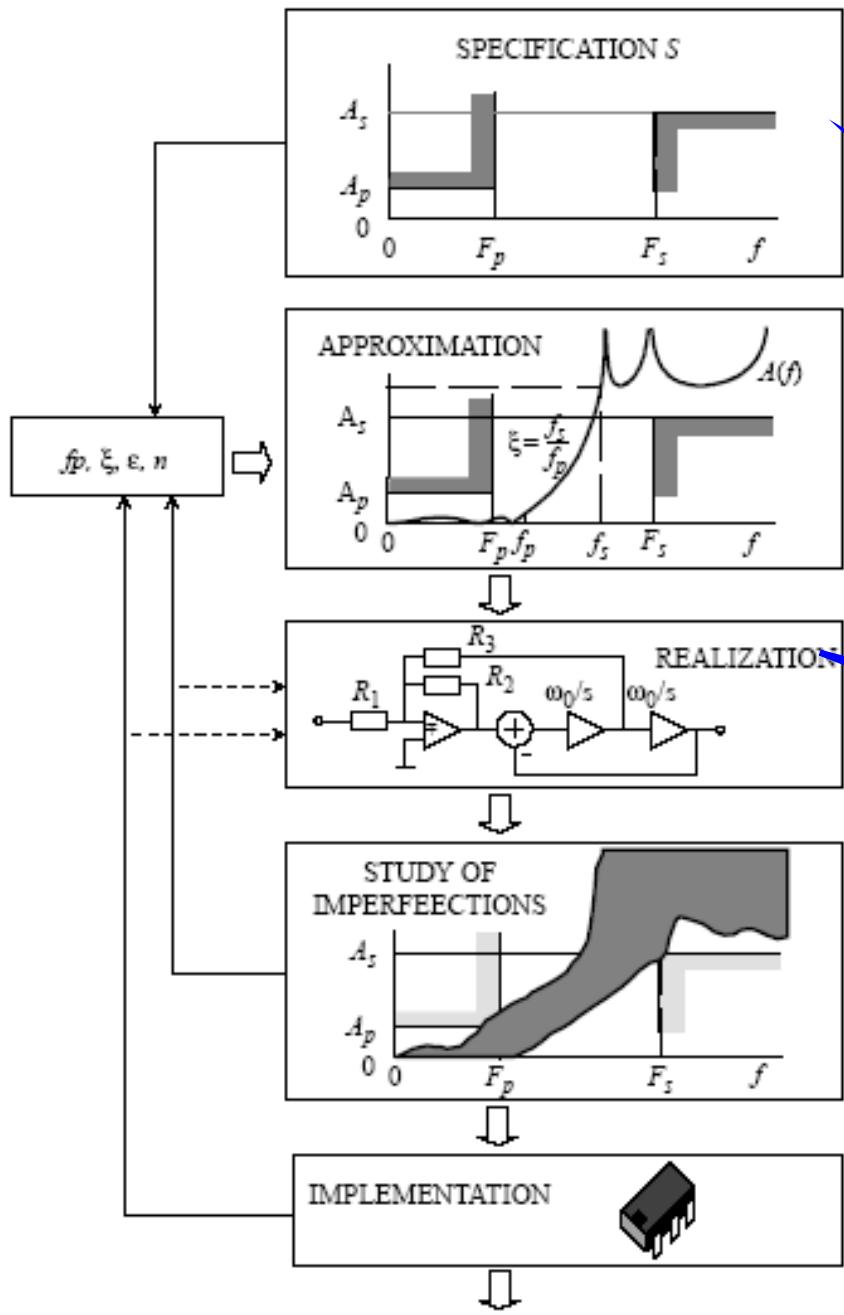


SPECIFIKACIJE ZA FILTAR  
PROPUSNIK NISKIH  
UČESTANOSTI



SPECIFIKACIJE ZA FILTAR  
PROPUSNIK VISOKIH  
UČESTANOSTI

# Od specifikacija do realizacije



Specifikacije

Sinteza

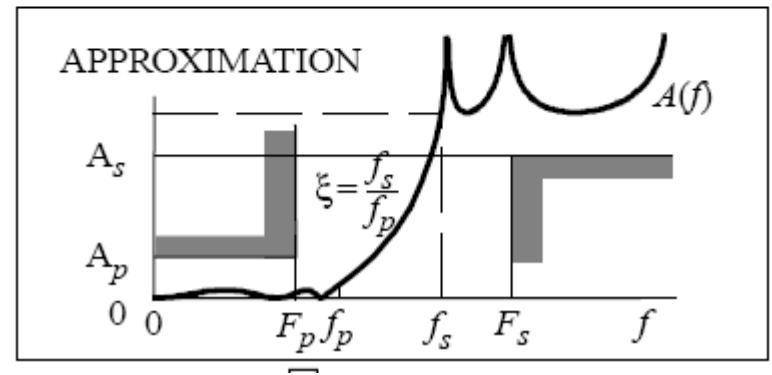
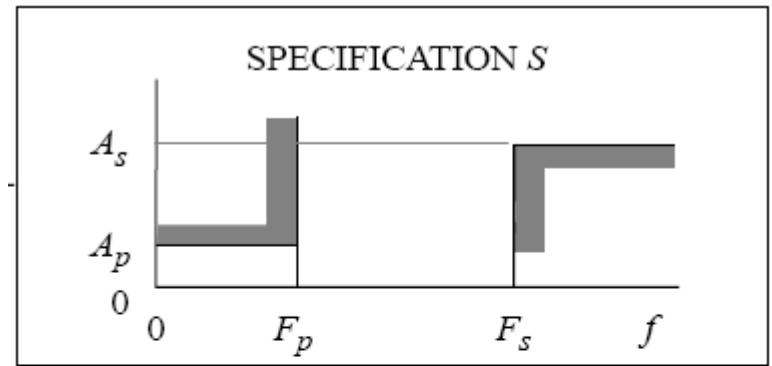
# Specifikacije

- Definišu se dozvoljene **tolerancije** u određenim frekvencijskim opsezima

$H(s)$  je racionalna funkcija kompleksne frekvencije  
 $s = \delta + j\omega$ ,  $s = j2\pi f$

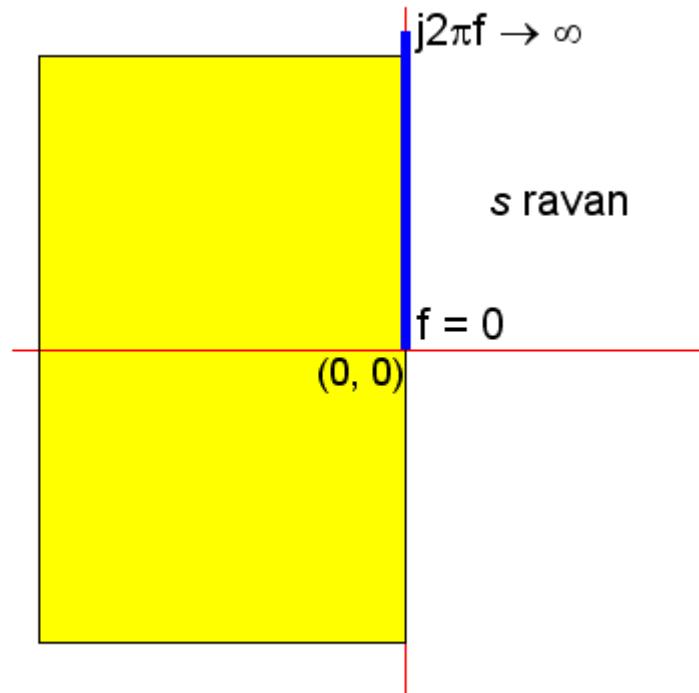
$$H(s) = \frac{\sum_{k=0}^M c_k s^k}{\sum_{k=0}^N d_k s^k} = \frac{C(s)}{D(s)}$$

$$a(f) = -20 \log(|H(j2\pi f)|)$$



# Frekvencijski odziv

$$H(s) = \frac{\sum_{k=0}^M c_k s^k}{\sum_{k=0}^N d_k s^k} = \frac{C(s)}{D(s)}$$

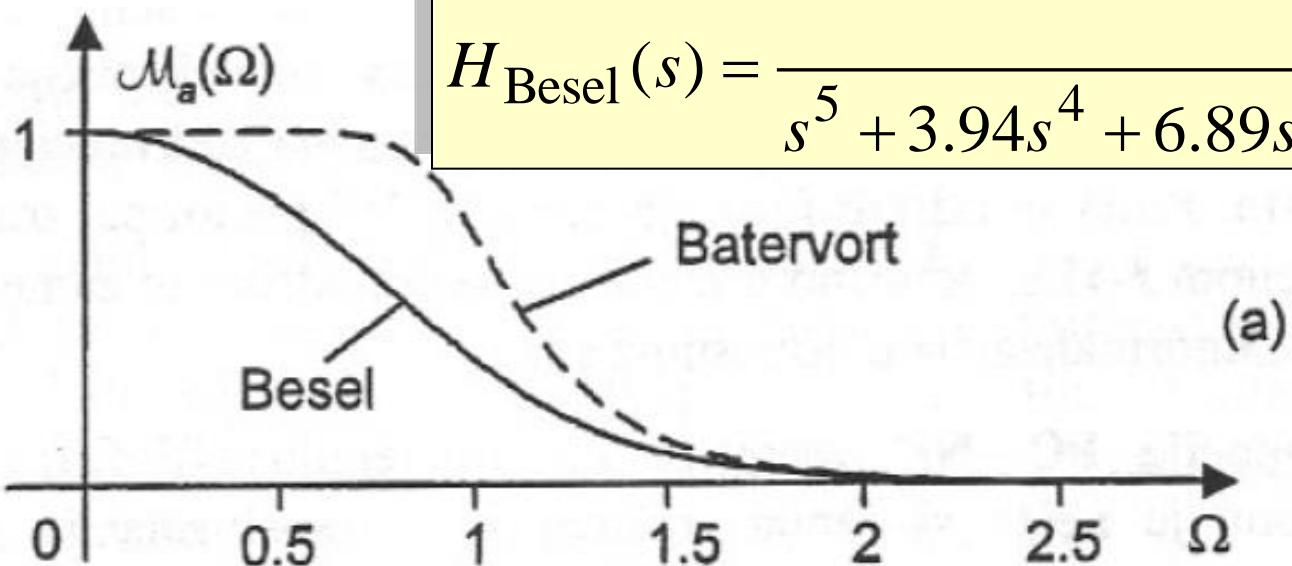


$$H(j2\pi f)$$

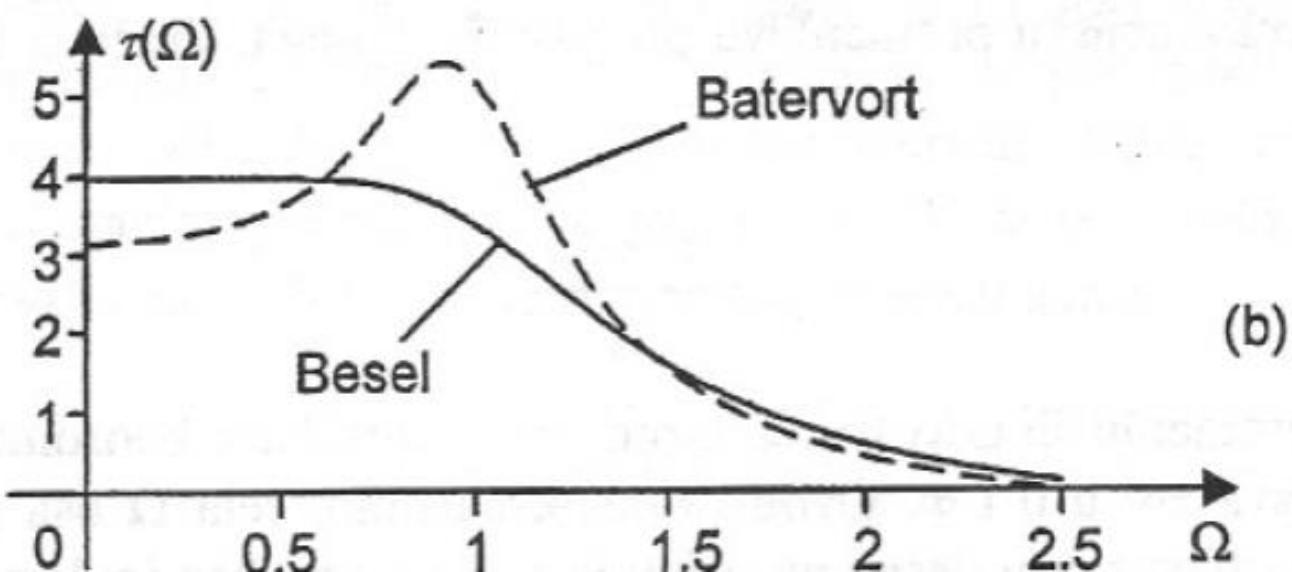
$$0 \leq f \leq \infty$$

$$H_{\text{Batervort}}(s) = \frac{1}{s^5 + 3.24s^4 + 5.24s^3 + 5.24s^2 + 3.24s + 1}$$

$$H_{\text{Besel}}(s) = \frac{1}{s^5 + 3.94s^4 + 6.89s^3 + 6.78s^2 + 3.81s + 1}$$

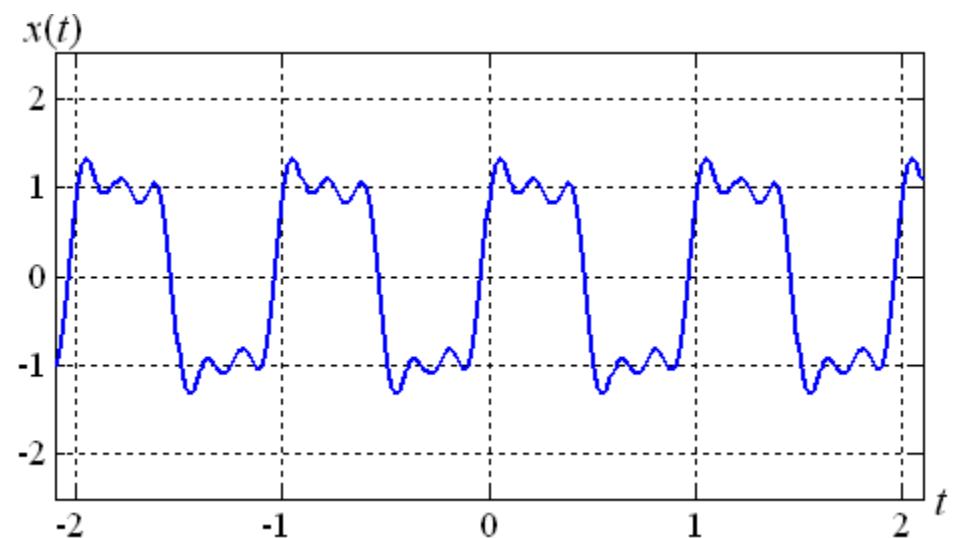
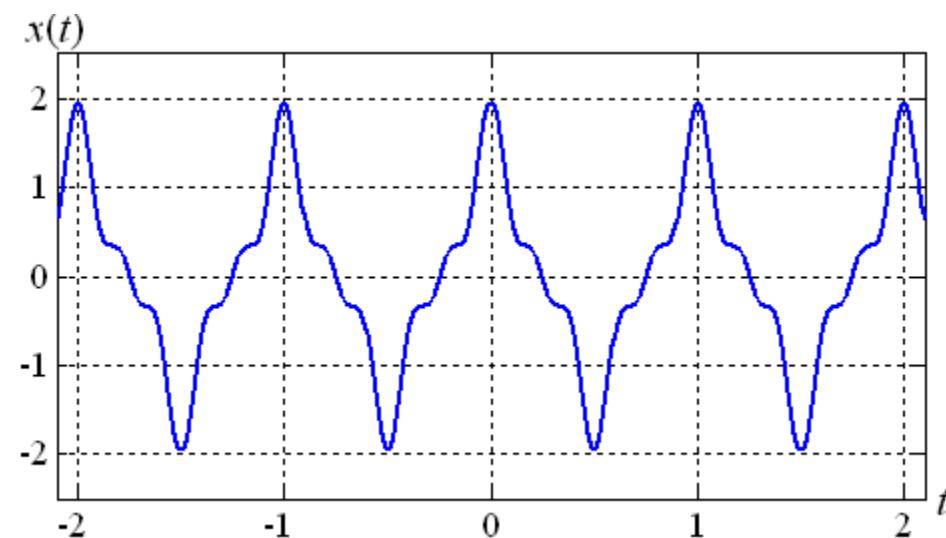
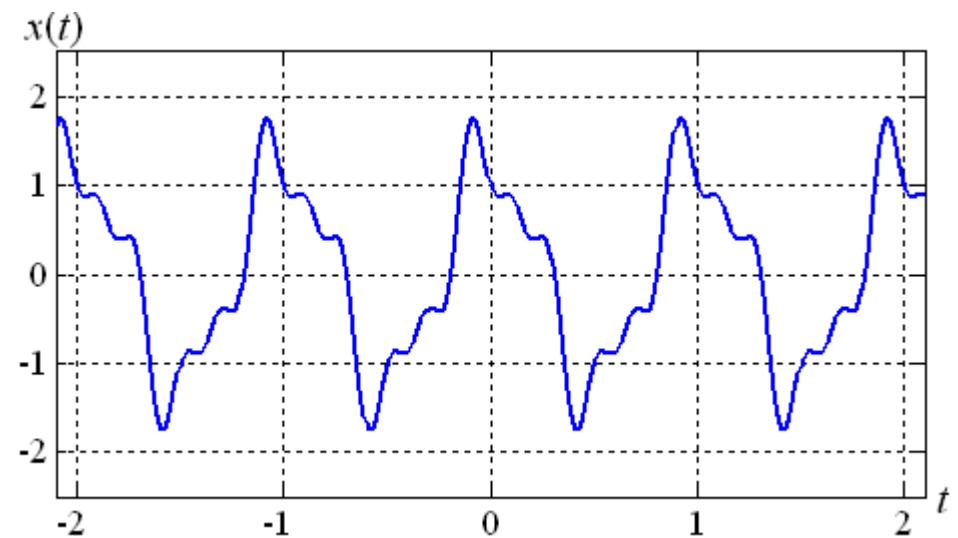
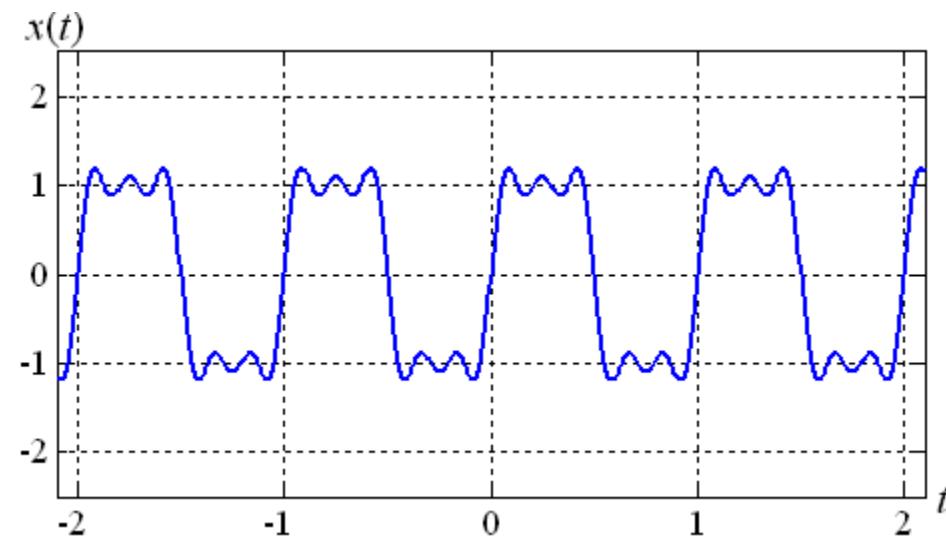


(a)

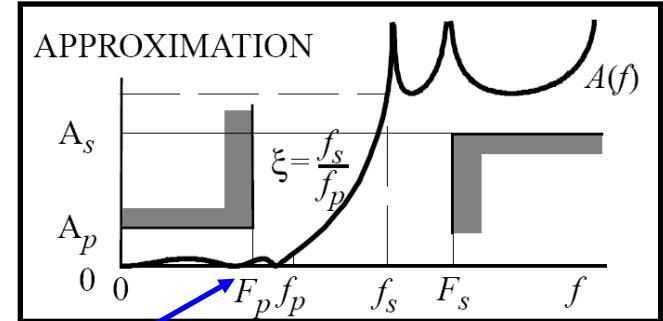


(b)

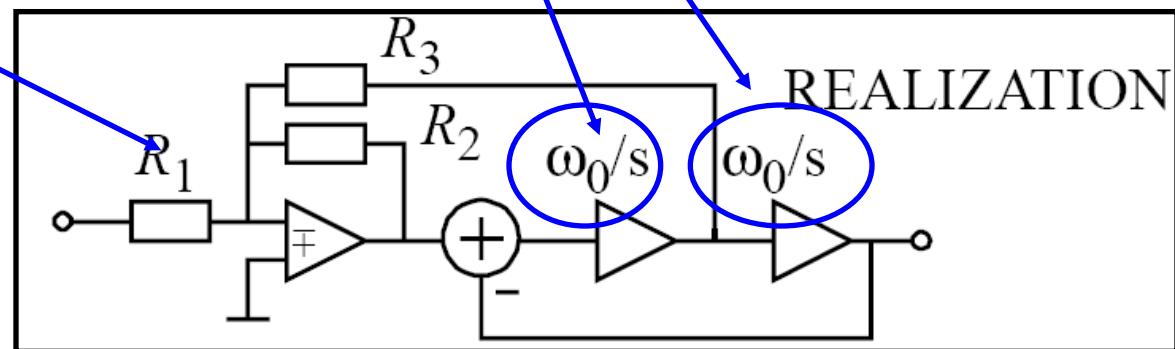
# Uticaj fazne karakteristike



# Sinteza



- Naći funkciju prenosa takvu da je racionalna funkcija po s što nižeg reda i da amplitudska karakteristika zadovoljava specifikacije
- da se koristi minimalan broj elemenata u realizaciji



# Analogni filter

- **Analogni filter** je električno kolo koje se koristi da pojača ili oslabi sinusoidalne signale ili signale koji zauzimaju određeni frekvencijski opseg
- Opseg učestanosti u kome se signali pojačavaju ili propuštaju bez većih slabljenja naziva se **propusni opseg**
- Opseg učestanosti u kome se signali značajnije slabe, naziva se **nepropusni opseg**
- **Specifikacije** su zahtevi u pogledu minimalnog dozvoljenog ili maksimalnog slabljenja ili pojačanja signala, u nekom opsegu učestanosti, a granice opsega su granične učestanosti
- **Projektovanje (sinteza)** analognog filtra je proces u kome konstruišemo kolo, odnosno izračunavamo vrednosti elemenata tako da to kolo zadovolji specifikacije

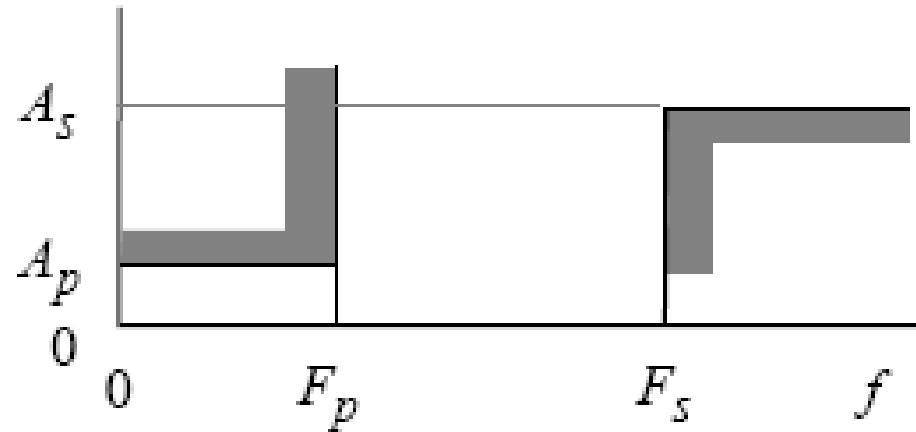
# Projektovanje - sinteza

- Projektovanje se sastoji od
  - Aproksimacije
  - Realizacije
  - Analiza nesavršenosti
  - Implementacije
- Broj električnih kola koji može da se napravi a da zadovolji specifikacije je beskonačan
- Kako izabrati optimalno rešenje?

# Filtar propusnik niskih učestanosti

- Propušta sinusoidalne signale čija je učestanost u opsegu  $0 \leq f \leq f_p$
- Slabi signale čija je učestanost  $f \geq F_s > F_p$   
*to je analogni lowpass filter*
- Opseg učestanosti  $0 \leq f \leq f_p$  je propusni opseg
- Opseg učestanosti  $f \geq F_s > F_p$  je nepropusni opseg
- $F_p$  je granica propusnog opsega (*passband edge frequency*)
- $F_s$  je granica nepropusnog opsega (*stopband edge frequency*)
- Slabljenje u propusnom opsegu ne sme biti veće izvan opsega  $0 - A_p$  u dB
- Slabljenje u nepropusnom opsegu ne sme biti manje od  $A_s$  u dB,  $A_s > 0$
- $A_p$  je *maximum passband attenuation*
- $A_s$  je *minimum stopband attenuation*
- Lista  $S = \{F_p, F_s, A_p, A_s\}$  je **specifikacija lowpass filtra**

# Tolerancije karakteristike slabljenja



$$0 \leq A(f) \leq A_p \text{ za } 0 \leq f \leq F_p$$

$$A(f) = -20 \log(\bullet^*(f))$$

$$S = \{F_p, F_s, A_p, A_s\}$$

$$A_s \leq A(f) \leq +\infty \text{ za } F_s \leq f < +\infty$$

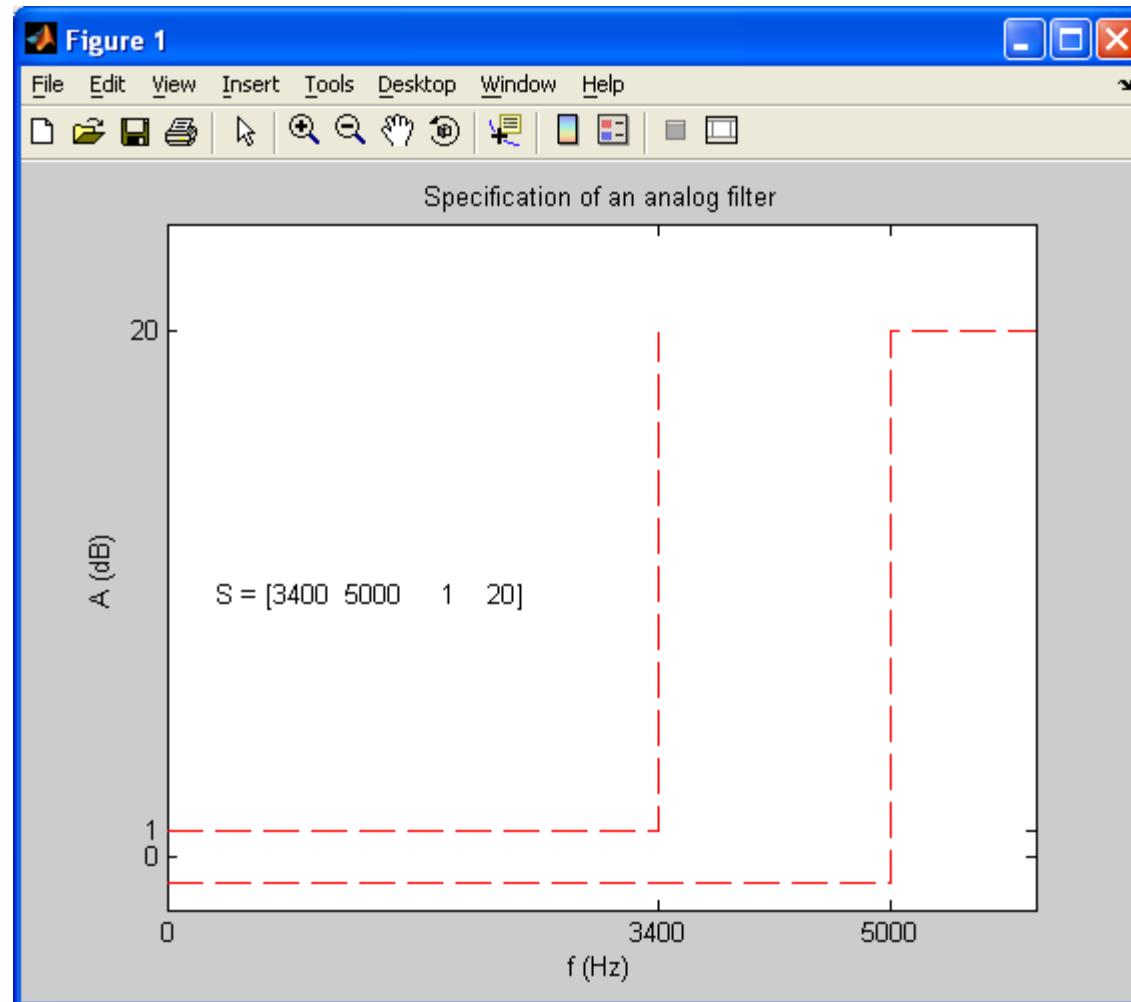
Propusni opseg

Nepropusni opseg

# Primer projektovanja

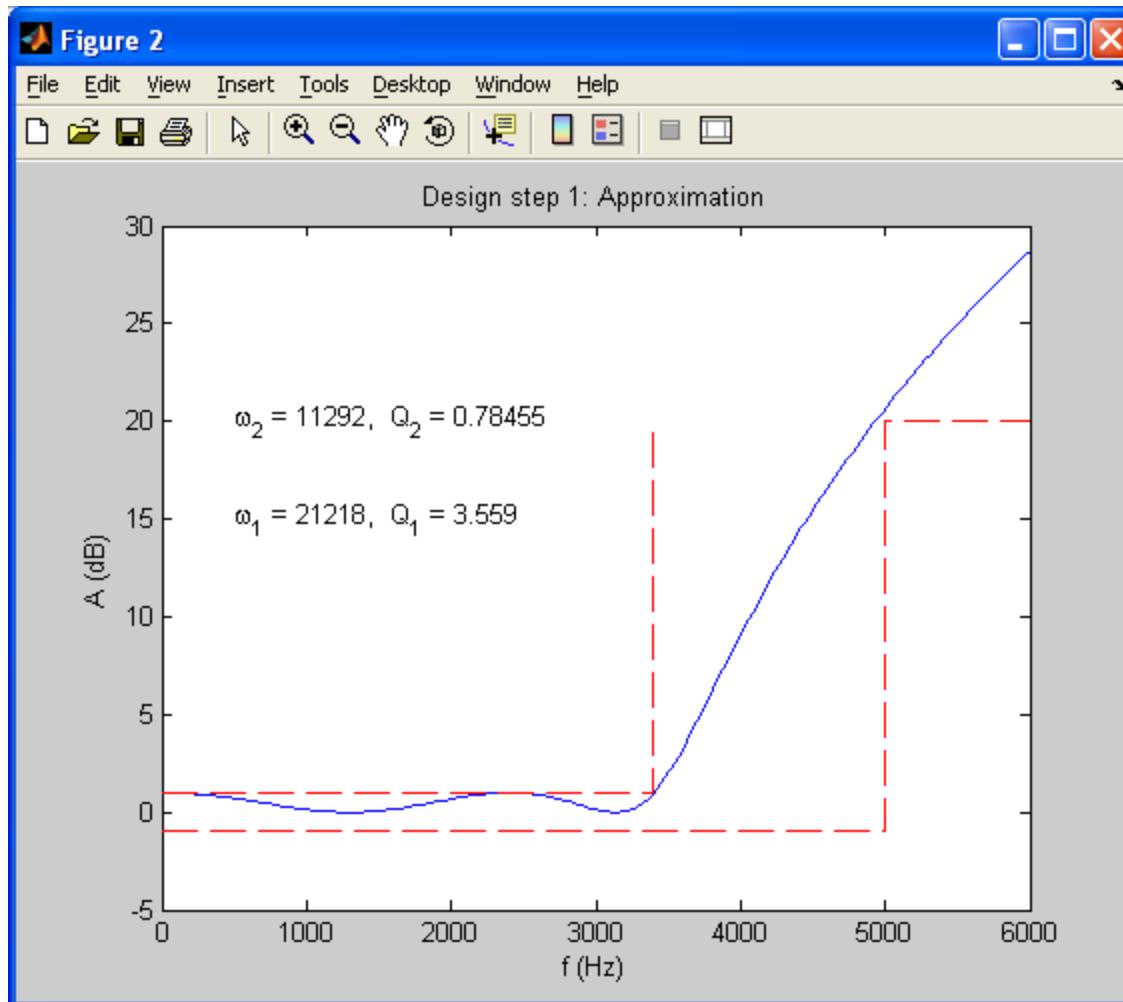
- Specifikacije
- 1: aproksimacija – izbor Čebiševljeve
- 2: realizacija – kaskada bikvada
- 3: analiza nesavršenosti – zaokruživanje vrednosti
- Ponavljanje projektovanja ako nije zadovoljen spek
  - 1: aproksimacija
  - 2: realizacija
  - 3: analiza nesavršenosti
- 4: implementacija
- MATLAB i dokumentacija

# Start sa specifikacijama

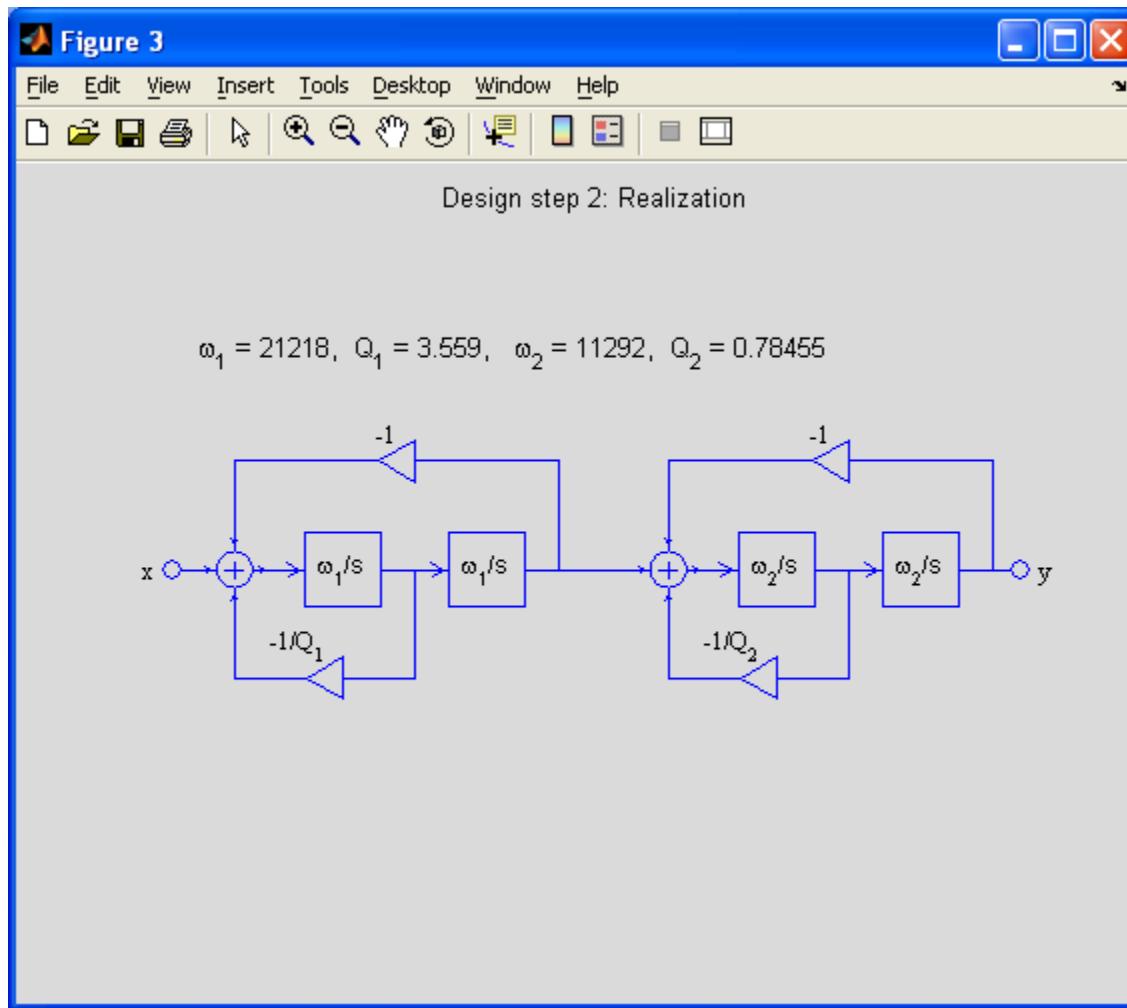


# 1: aproksimacija

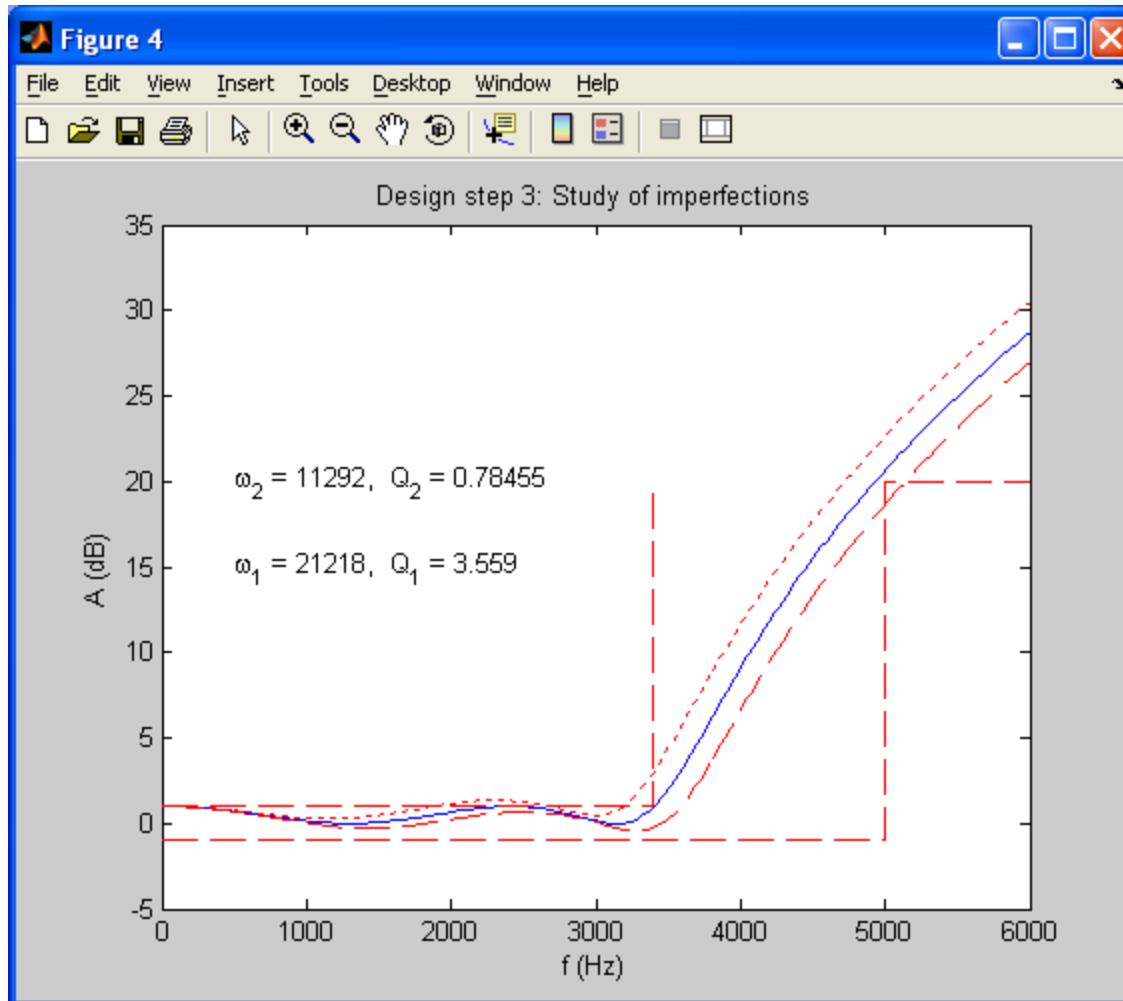
## Izbor Čebiševljeve aproksimacije tip I



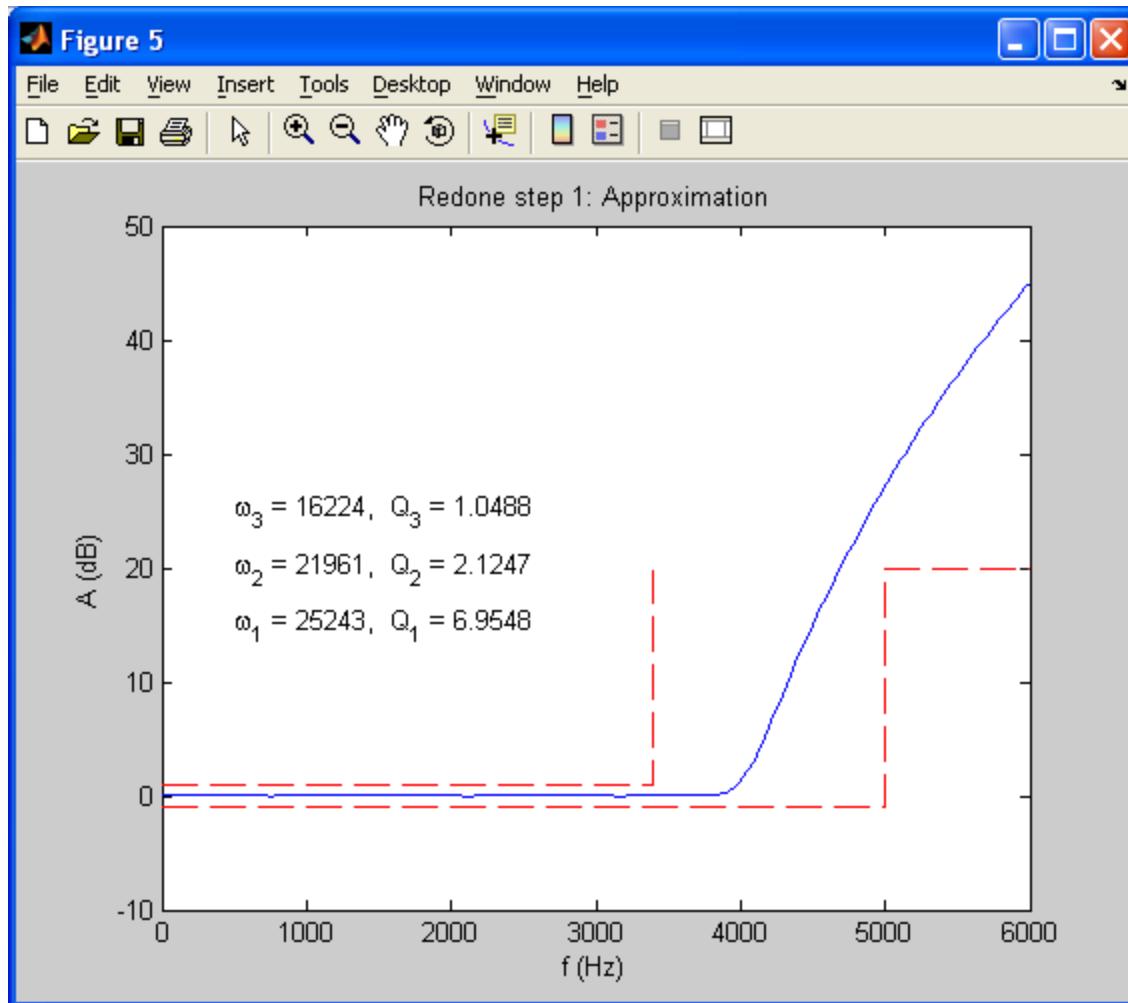
## 2: realizacija (sinteza) Kaskada programabilnih sekcija drugog reda (biquads)



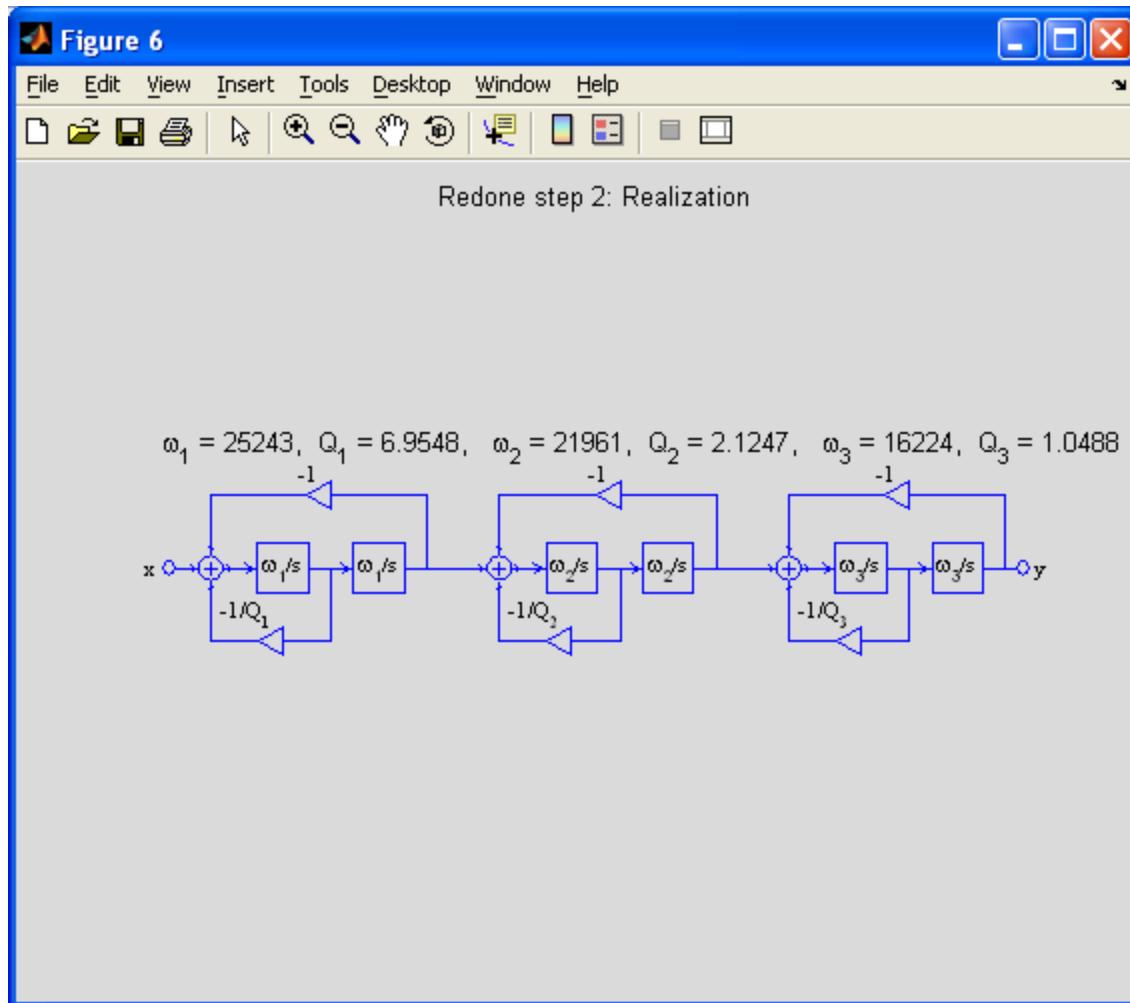
# 3: Analiza nesavršenosti analiza osetljivosti



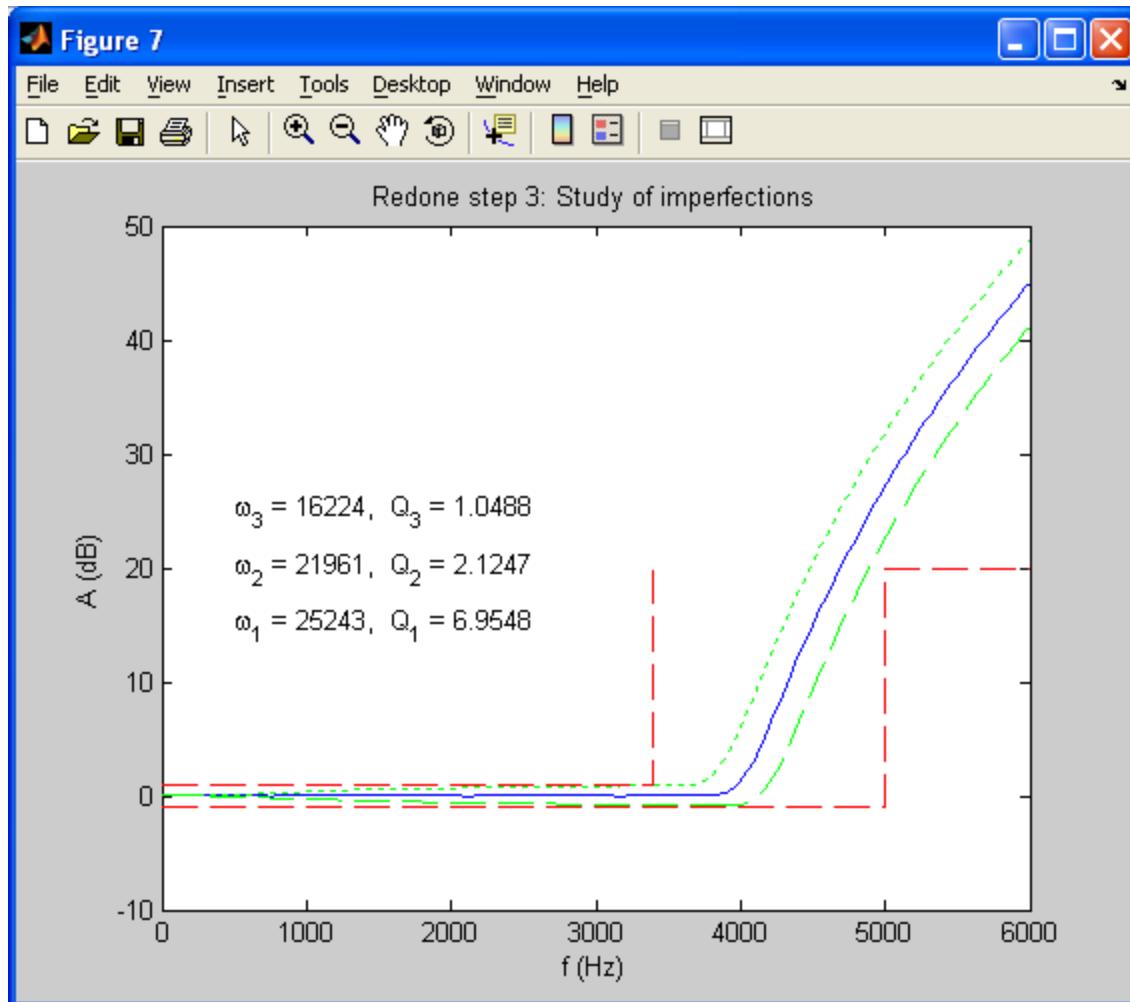
# Ponovo 1: aproksimacija povećanje reda funkcije prenosa



# Ponovo 2: realizacija

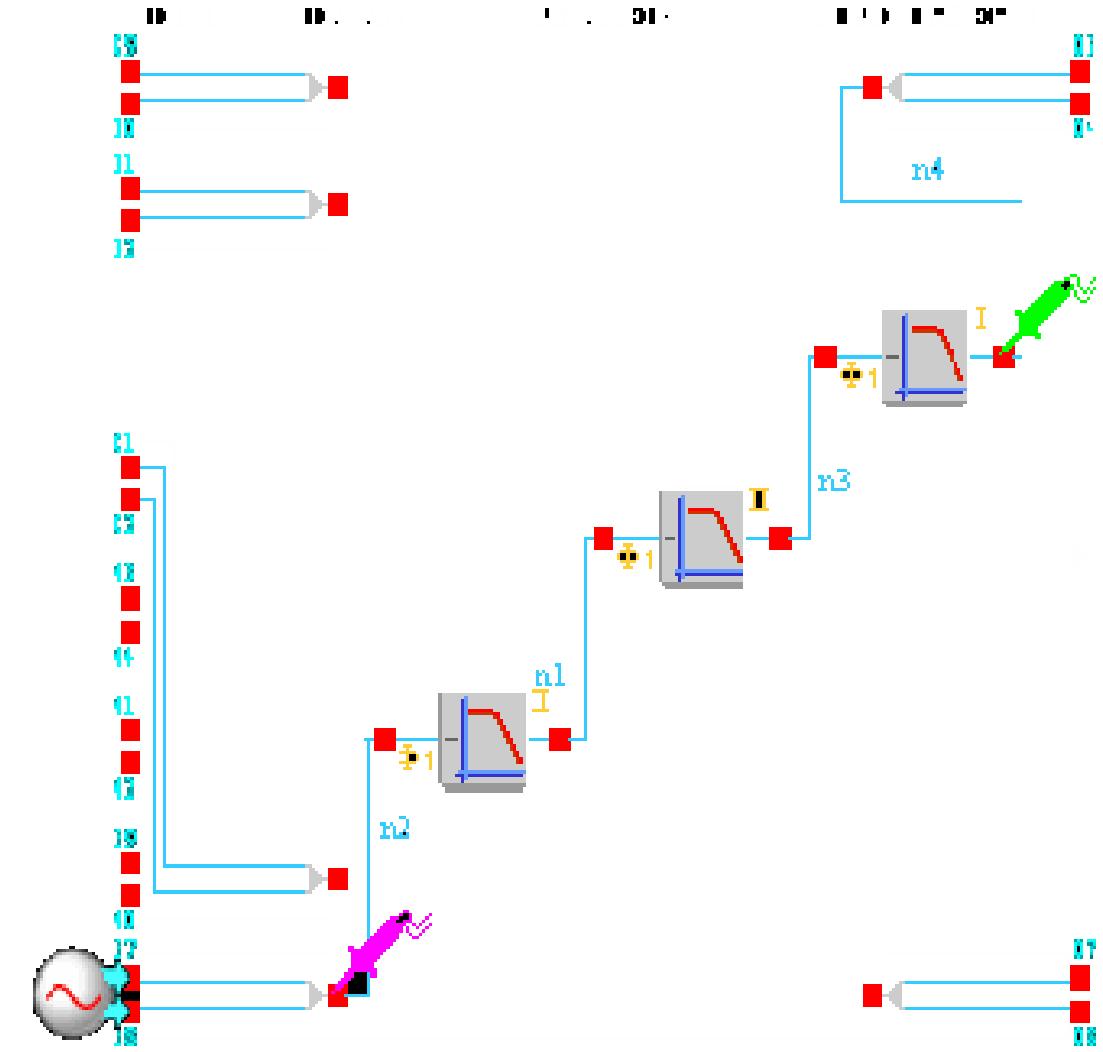


# Ponovo 3: analiza nesavršenosti

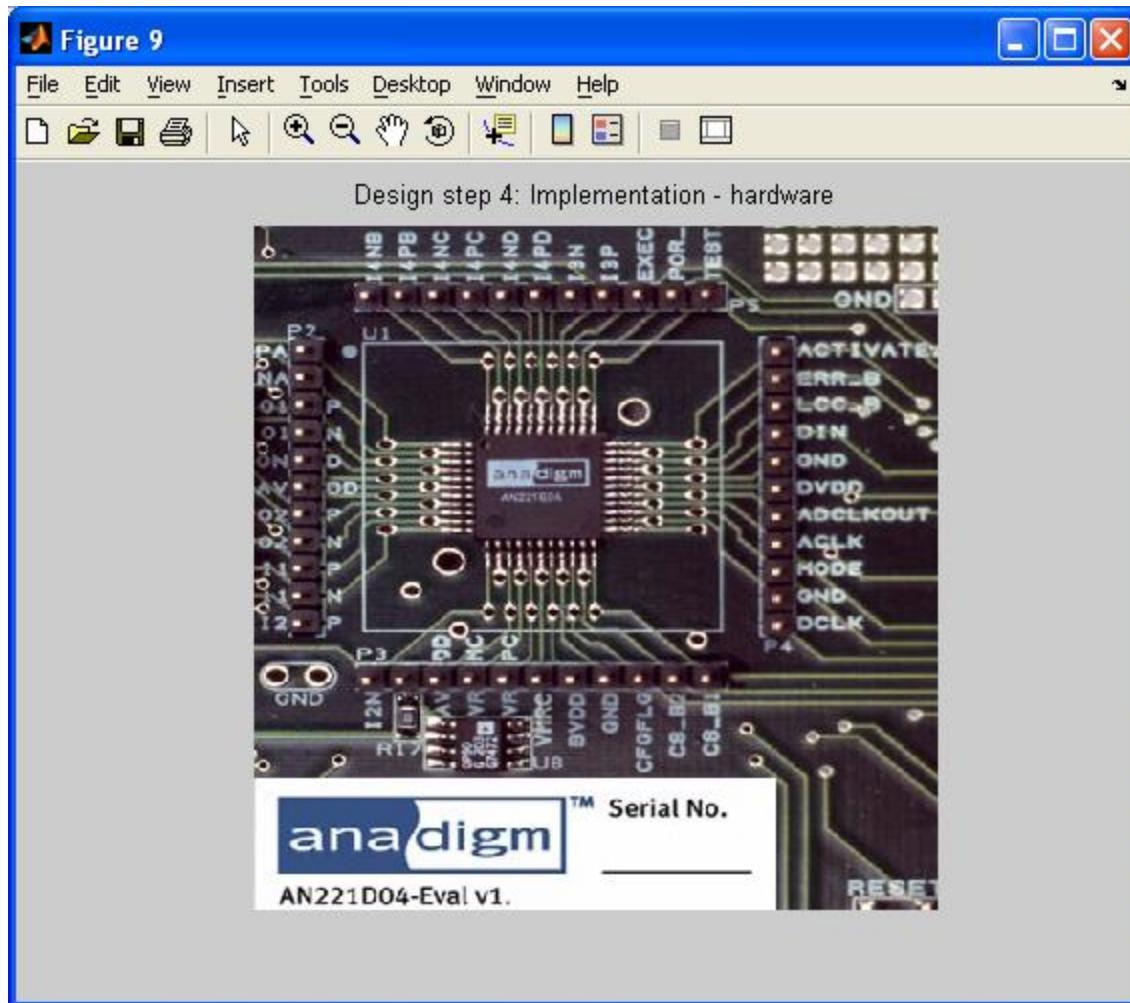


# 4: implementacija (1)

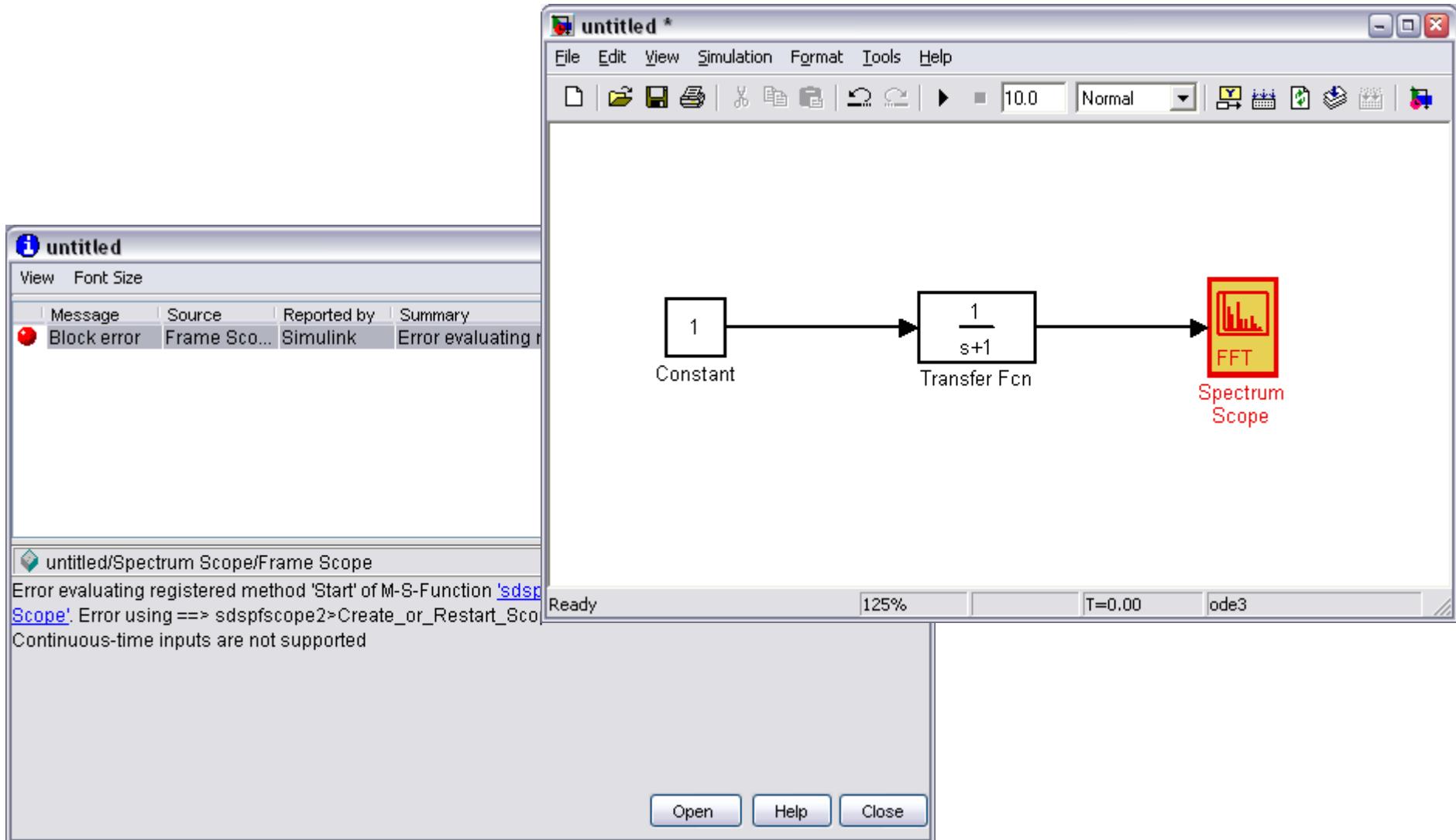
Design step 4: Implementation - block diagram



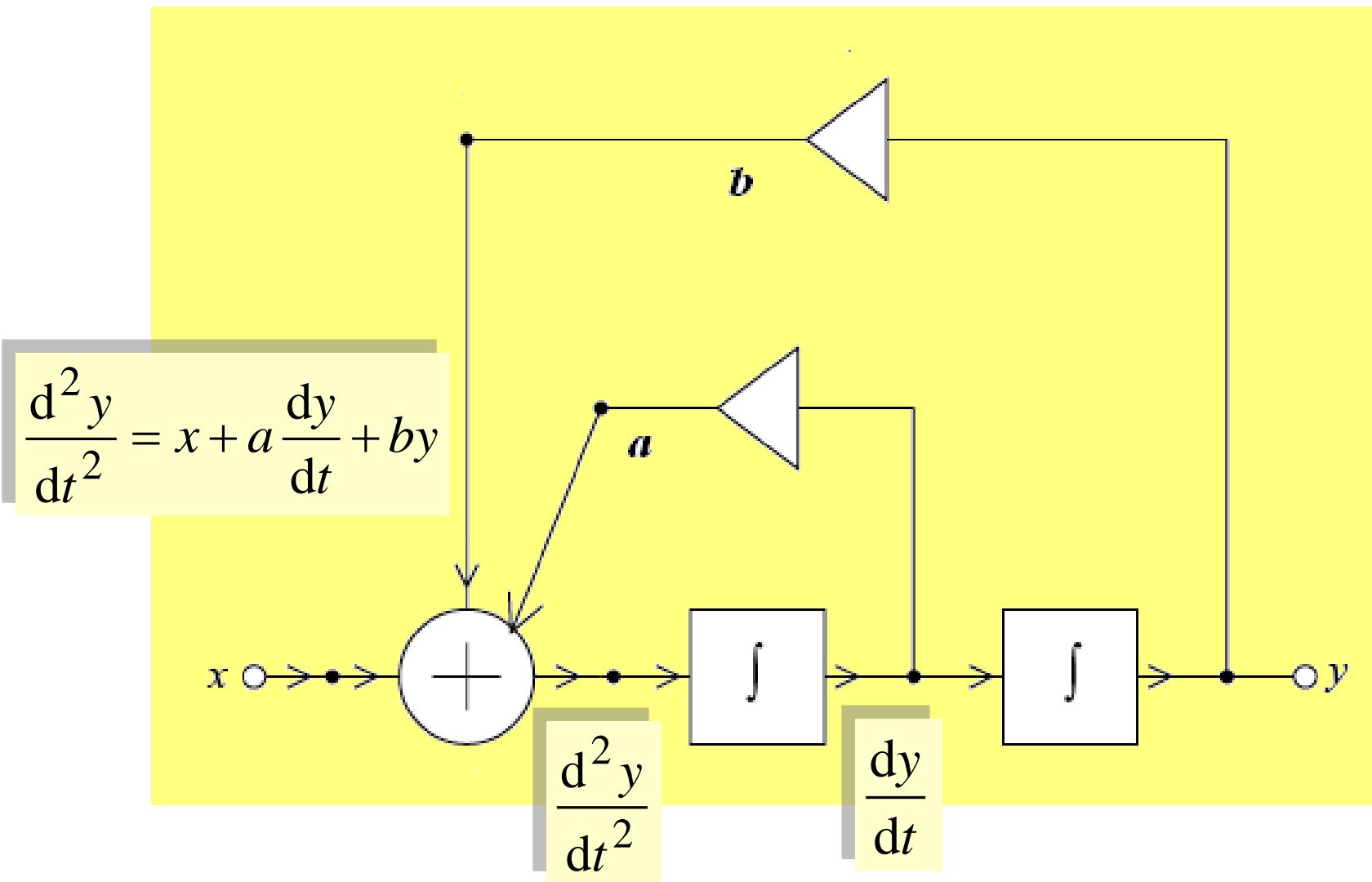
# 4: implementacija (2)



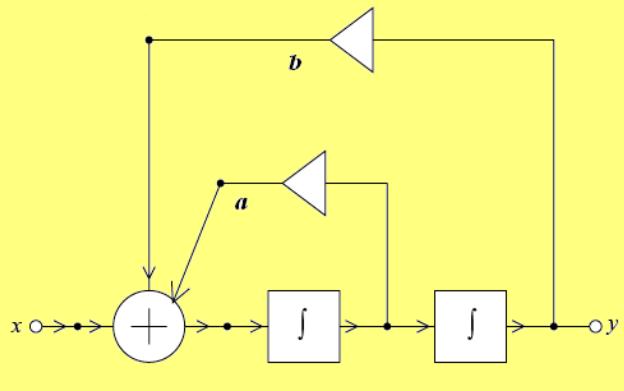
# Simulink ne podržava analizator spektra za kontinualne signale



# Kontinualni sistemi



# Primena Laplasove transformacije



Funkcija prenosa

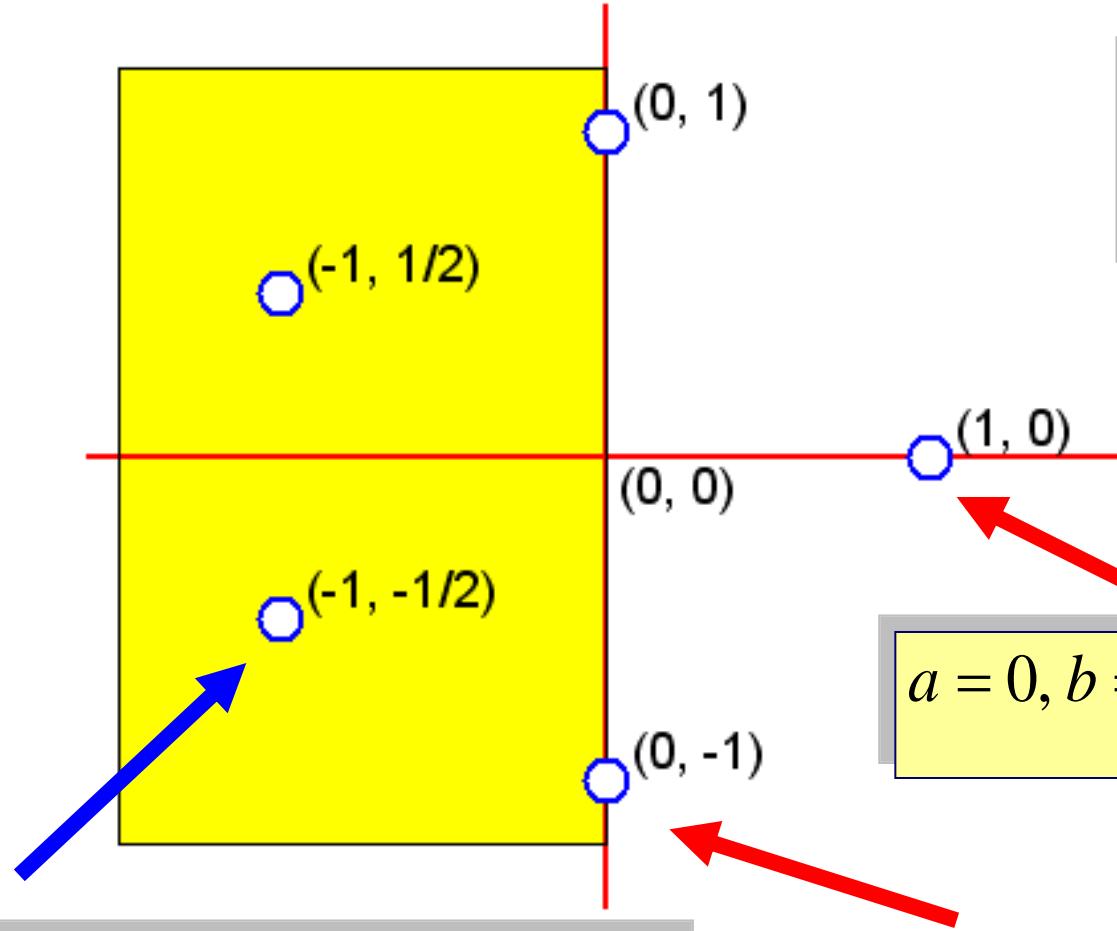
$$\frac{d^2y}{dt^2} = x + a \frac{dy}{dt} + by$$

$$s^2 Y(s) = X(s) + a s Y(s) + b Y(s)$$

$$(s^2 - a s - b)Y(s) = X(s)$$

$$\frac{Y(s)}{X(s)} = \frac{1}{s^2 - a s - b}$$

# Polovi funkcije prenosa u s ravni



$$\frac{1}{s^2 - as - b}$$

$$a = 0, b = 1 \rightarrow \lim_{t \rightarrow +\infty} y(t) = \pm\infty$$

$$\text{Re}(\text{pol}) < 0 \rightarrow \lim_{t \rightarrow +\infty} y(t) = 0$$

$$a = 0, b = -1 \rightarrow y(t) = \sin(t)$$

# Transformacije

- Laplasova transformacija impulsnog odziva

$$H(s) = \int_{-\infty}^{\infty} h(t)e^{-st} dt$$

# Funkcije prenosa

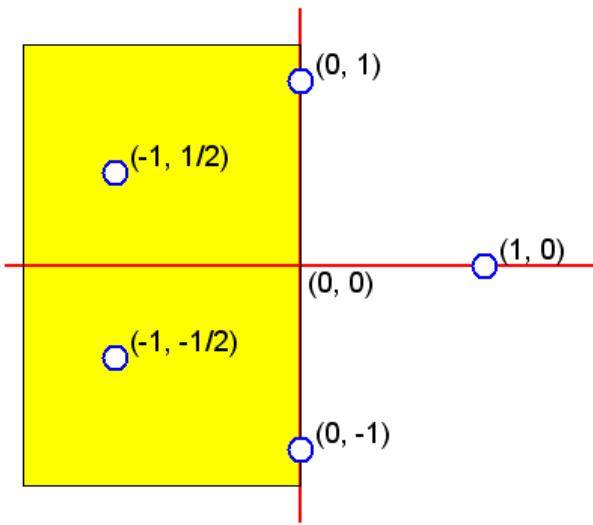
- Racionalna funkcija  
kompleksne  
frekvencije  $s=\delta+j\Omega$

$$H(s) = \frac{\sum_{k=0}^M c_k s^k}{\sum_{k=0}^N d_k s^k} = \frac{C(s)}{D(s)}$$

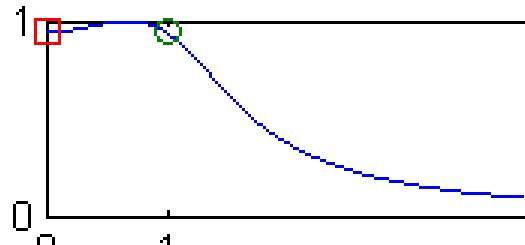
# Polovi funkcije prenosa

- Leva polovina kompleksne  $s$  ravni

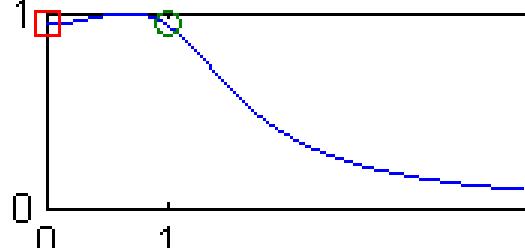
$$H(s) = \frac{C(s)}{D(s)}$$



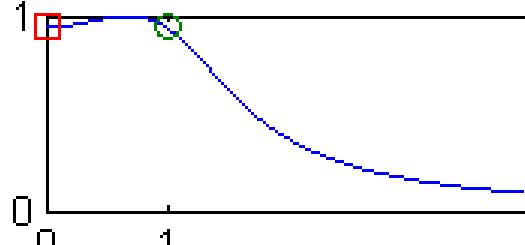
# Frekvencijske transformacije



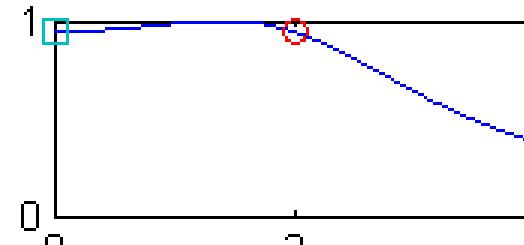
$$s \rightarrow \frac{s}{\Omega_n}$$



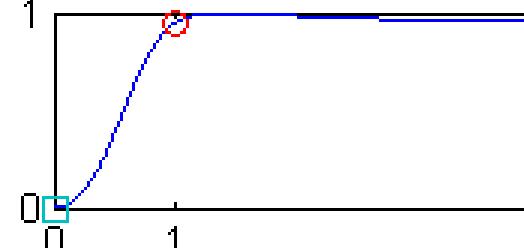
$$s \rightarrow \frac{1}{s}$$



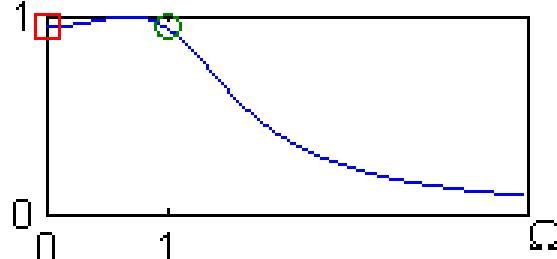
$$s \rightarrow \frac{s^2 + \Omega_0^2}{s}$$



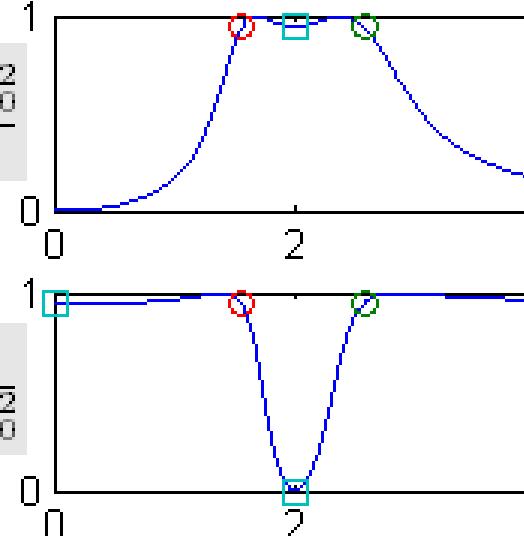
$$s \rightarrow j\Omega$$



$$\Omega_0 = \sqrt{\Omega_{p1}\Omega_{p2}}$$



$$s \rightarrow \frac{s}{s^2 + \Omega_0^2}$$



$$\Omega_0 = \sqrt{\Omega_{a1}\Omega_{a2}}$$

# Transformacije NF prototipa

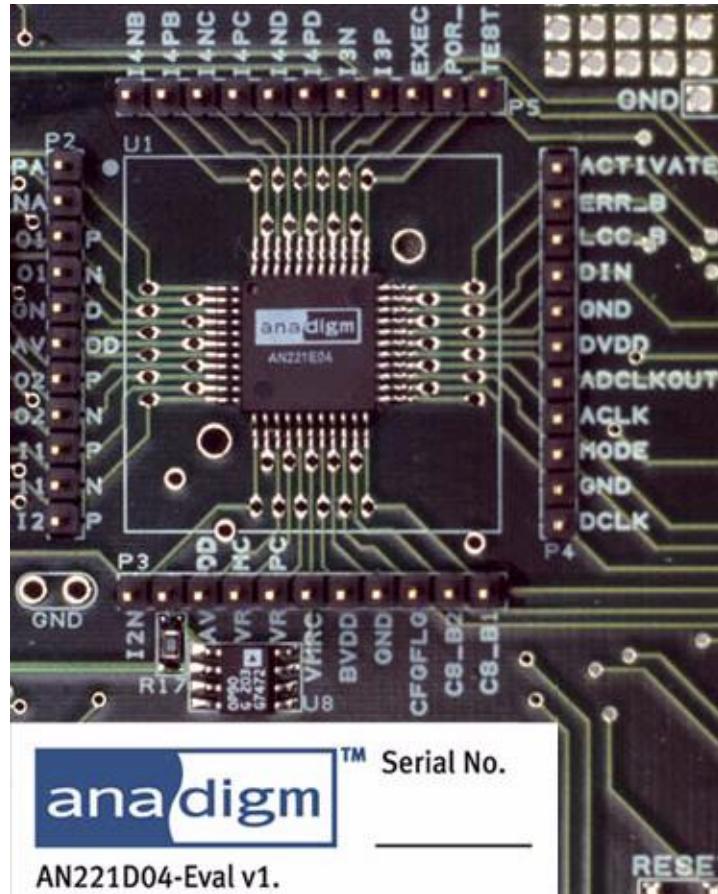
- Transformacija NF-NF prototip  $s \rightarrow s/\Omega_n$
- Transformacija VF-NF prototip  $s \rightarrow 1/s$
- Transformacija PO-NF prototip  
 $s \rightarrow (s^2 + \Omega_0^2)/s$
- Transformacija NO-NF prototip  
 $s \rightarrow s/(s^2 + \Omega_0^2)$

# Primer transformacije

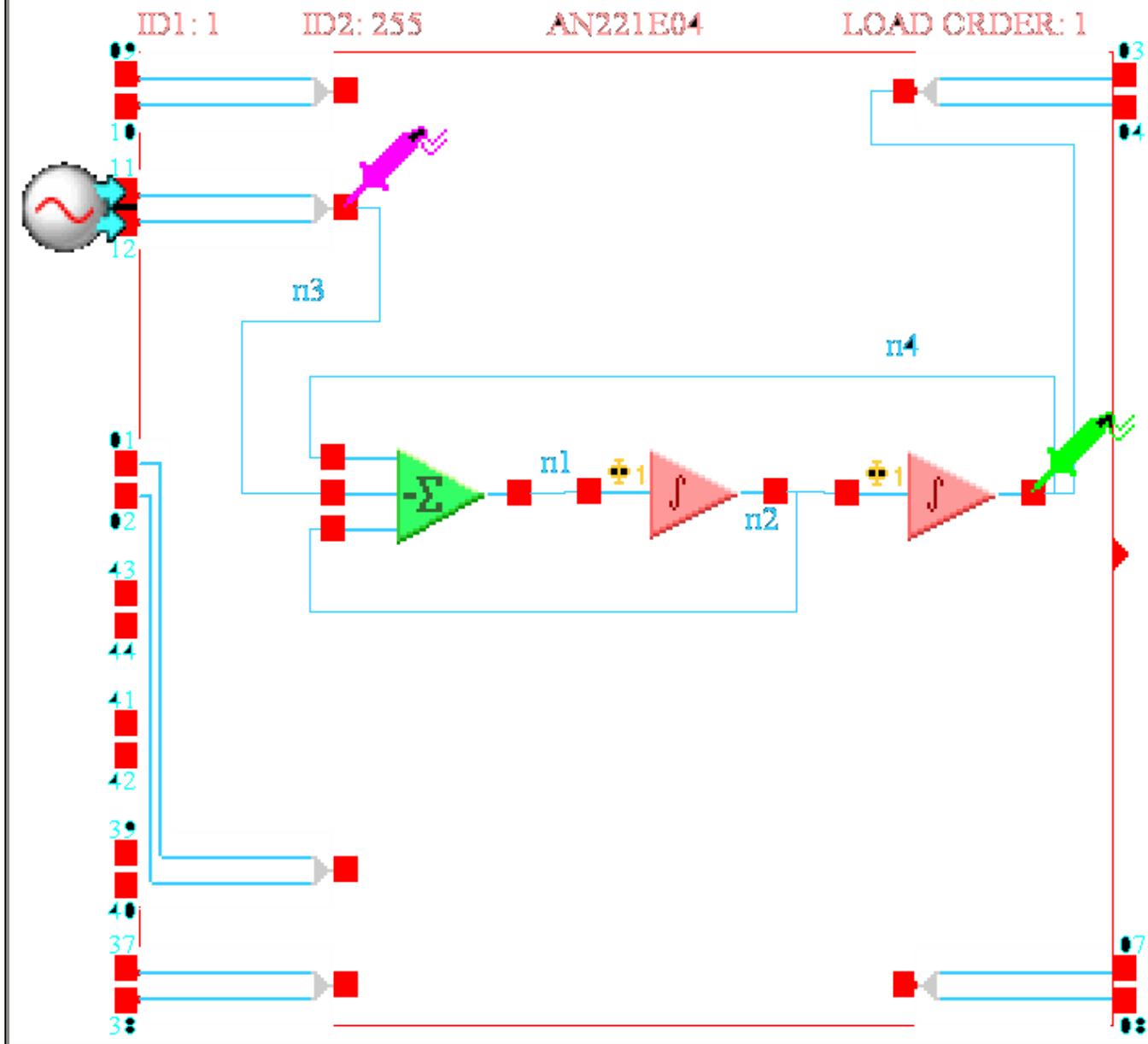
$$H_{\text{NF}} = \frac{1}{s^2 + 2s + 3} \Big|_{s \rightarrow \frac{s^2+1}{s}} \rightarrow H_{\text{PO}} = \frac{s^2}{s^4 + 2s^3 + 5s^2 + 2s + 3}$$

*H je racionalna funkcija*

# Hardverska implementacija



# Sistem sa integratorima



## Signal Generator Control



## Propusni opseg SIMULACIJA

### Output

Differential

Sine Modulated



### Signal Data

Peak Amplitude

2 Volts

Differential Offset

0 Volts

Frequency

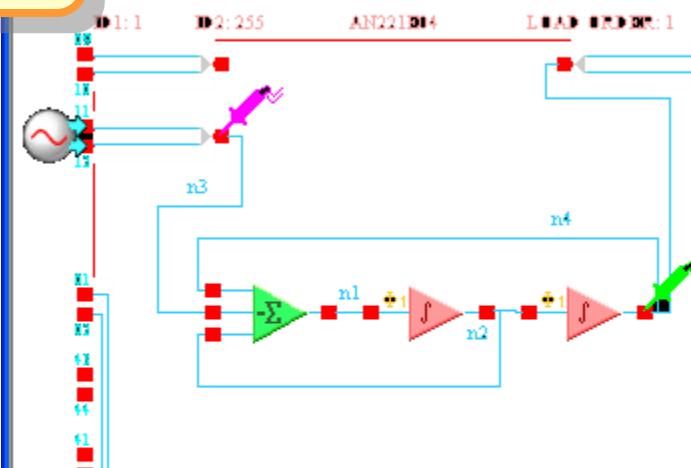
2.3 k Hz

Phase

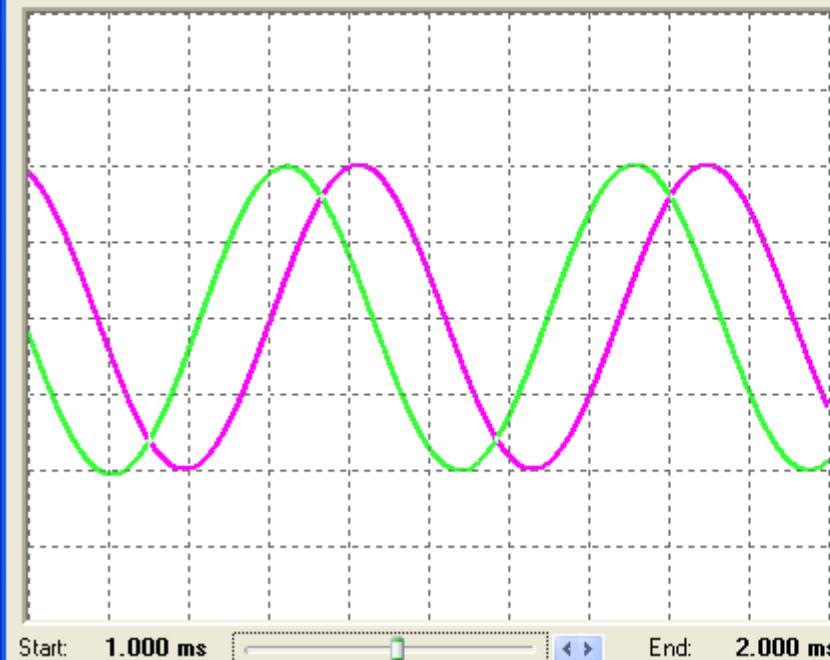
0 Degrees

Common Mode Offset

2 Volts



## Oscilloscope - Biquad.ad2



Display Data      Volts Per Division      Position      Voltage

Channel 1

1.0 V

▲

0

▼

Voltage

Channel 2

1.0 V

▲

0

▼

Voltage

Channel 3

1.0 V

▲

0

▼

Voltage

Channel 4

1.0 V

▲

0

▼

Voltage

Time Per Division:

100 µs

▲

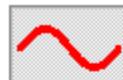
Time:

Grid

Cursor

Close

## Signal Generator Control



## Nepropusni opseg SIMULACIJA



### Output

Differential

Suspended



### Signal Data

Peak Amplitude

2 Volts

Differential Offset

0 Volts

### Frequency

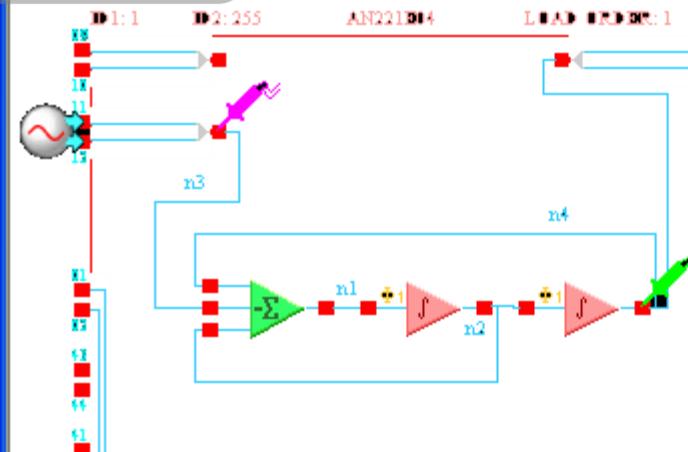
10k Hz

### Phase

0 Degrees

### Common Mode Offset

2 Volts



## Oscilloscope - Biquad.ad2



Display Data      Volts Per Division      Position      Voltage

Channel 1      1.0 V      0     

Channel 2      1.0 V      0     

Channel 3      1.0 V      0     

Channel 4      1.0 V      0     

Time Per Division: 100  $\mu$ s      Time:

Start: 1.000 ms

End: 2.000 ms

Grid

Cursor

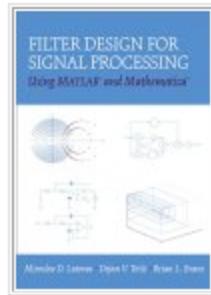
Close

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## MATLAB &amp; Simulink Based Books- Signal Processing

## Filter Design for Signal Processing Using MATLAB and Mathematica

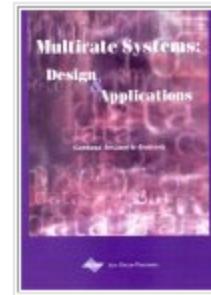


Written for courses in signal processing design. Using mathematical methods and the advanced filter design toolbox, the book covers various types of filters that can be used to solve sample problems. (The book is available in English.)

Companion Software: A set of MATLAB M-files is available.

## MATLAB &amp; Simulink Based Books- Signal Processing

## Multirate Systems: Design &amp; Applications

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ISBN: 1-930708-00-X

Language: English

Written for students and practicing engineers involved in multirate signal processing. Topics covered include multirate sampling rate conversion, subband coding, and design of multirate systems. The Signal Processing Toolbox is used to solve examples and filtering.

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## MATLAB &amp; Simulink Based Books- Chinese

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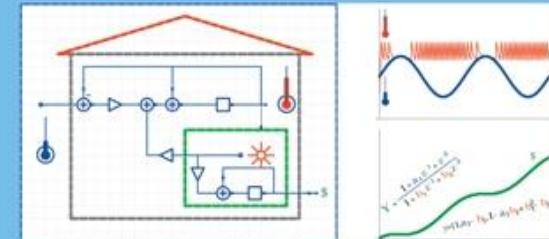
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